

# SMS-NLINV

## Simultaneous Imaging of Multiple Slices

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### Simultaneous Multi-Slice MRI Using Cartesian and Radial FLASH and Regularized Nonlinear Inversion: SMS-NLINV

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Dirk Voit, <sup>3</sup> Jens Frahm, <sup>2,3</sup> and Martin Uecker 

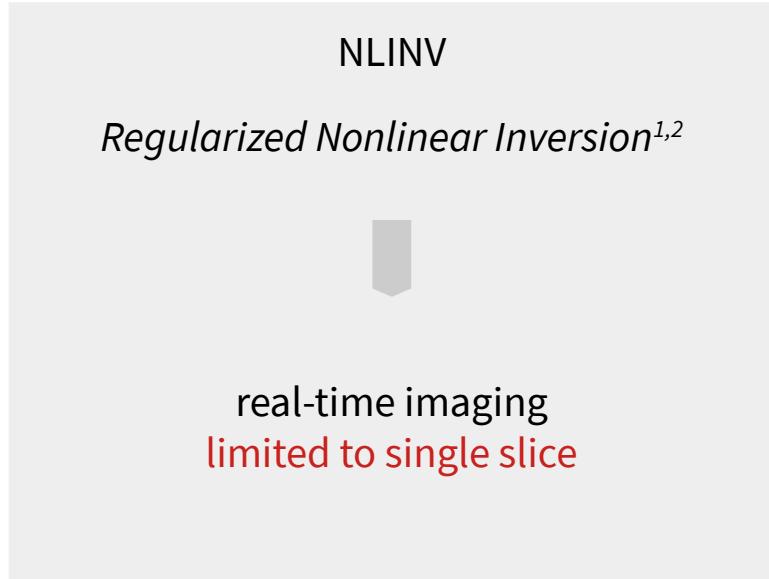
**Purpose:** The development of a calibrationless parallel imaging method for accelerated simultaneous multi-slice (SMS) MRI based on Regularized Nonlinear Inversion (NLINV), evaluated using Cartesian and radial fast low-angle shot (FLASH).  
**Theory and Methods:** NLINV is a parallel imaging method

consist of a calibration from reference lines followed by linear reconstruction (1–4). In contrast, Regularized Nonlinear Inversion (NLINV) (5) does not require a calibration step but simultaneously computes image content and coil sensitivities from all available data. Because



SMS-NLINV  
Motivation

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[1] Uecker et al., Magn. Reson. Med. (2008)

[2] Uecker et al., NMR Biomed (2010)

SMS-NLINV  
Motivation

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NLINV

*Regularized Nonlinear Inversion<sup>1,2</sup>*



real-time imaging  
**limited to single slice**

SMS

*Simultaneous Multi-Slice<sup>3</sup>*



less data demand  
time-consistent slices

[1] Uecker et al., Magn. Reson. Med. (2008)

[2] Uecker et al., NMR Biomed (2010)

[3] Larkman et al., Magn. Reson. Med. ( 2001)

SMS-NLINV  
Motivation

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NLINV

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SMS-NLINV

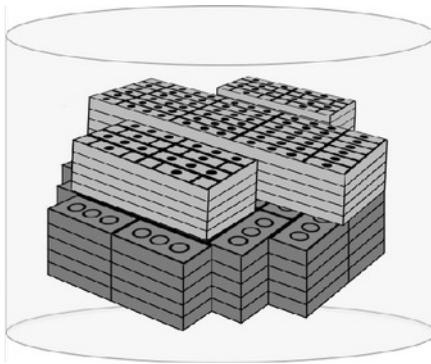
[1] Uecker et al., Magn. Reson. Med. (2008)

[2] Uecker et al., NMR Biomed (2010)

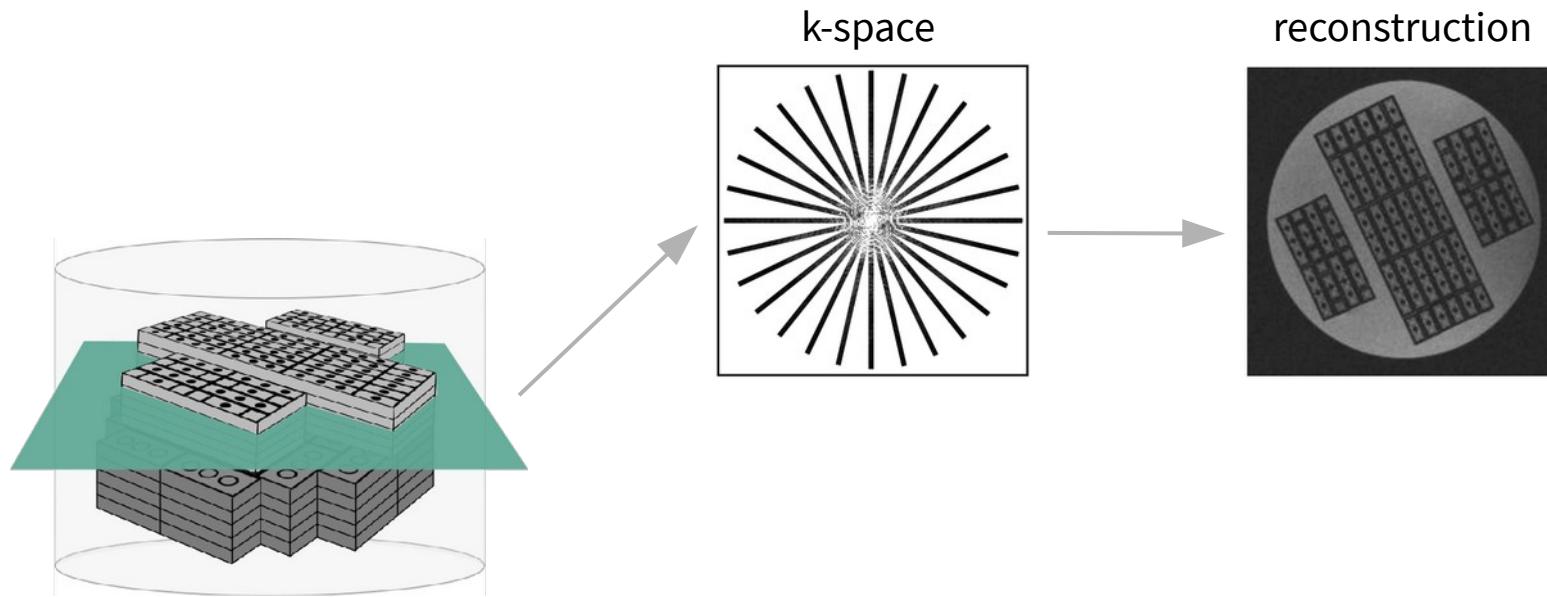
[3] Larkman et al., Magn. Reson. Med. (2001)

# Conventional Multi-Slice Imaging

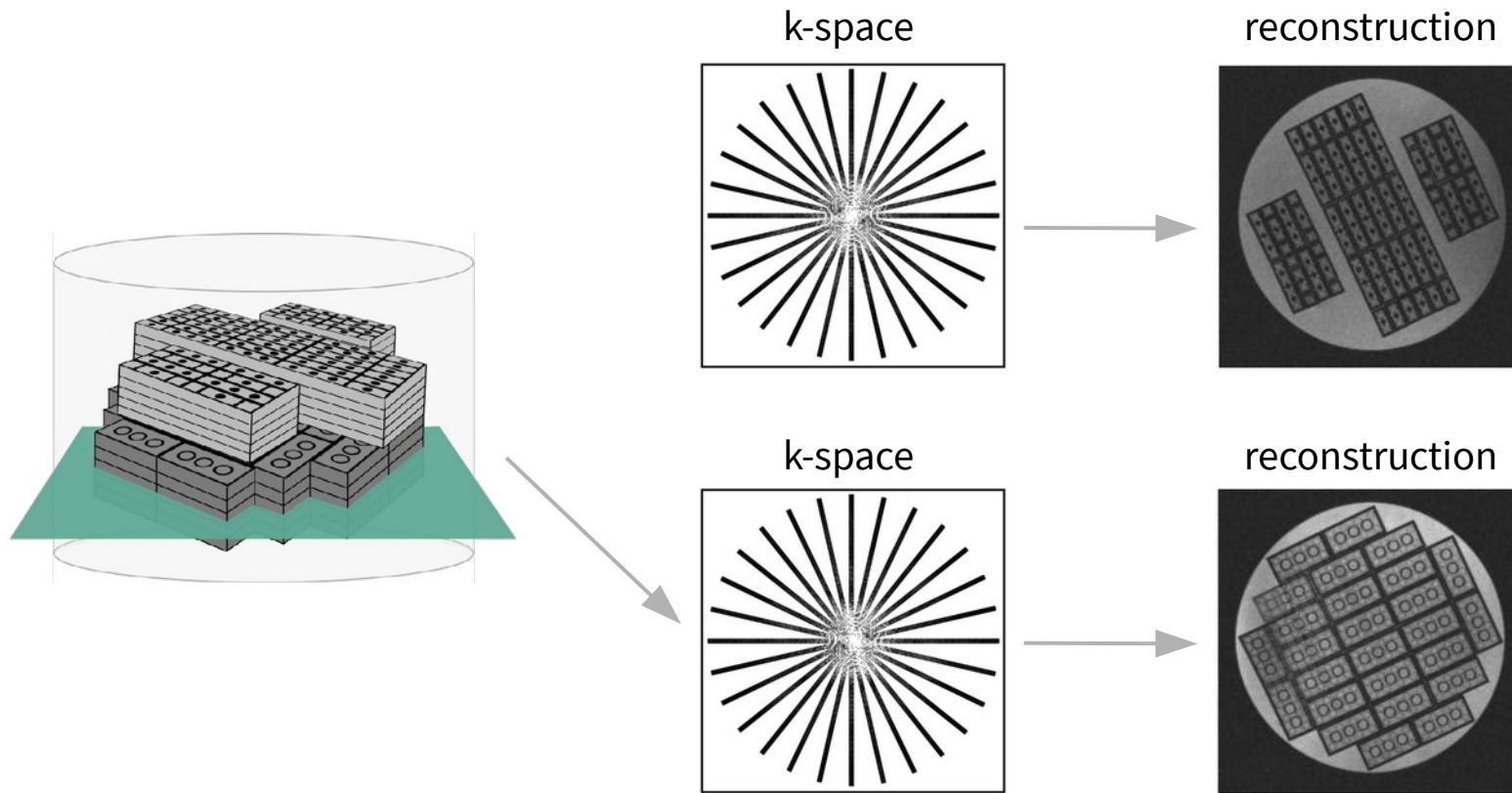
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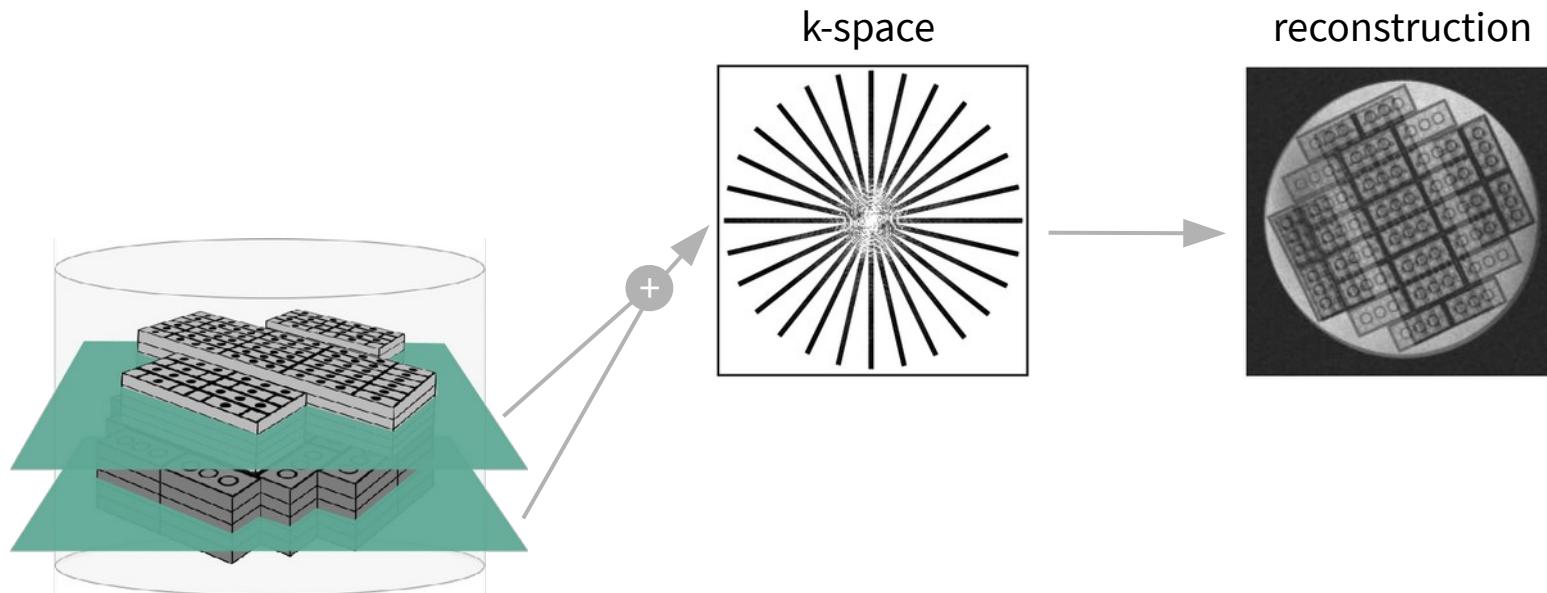
# Conventional Multi-Slice Imaging



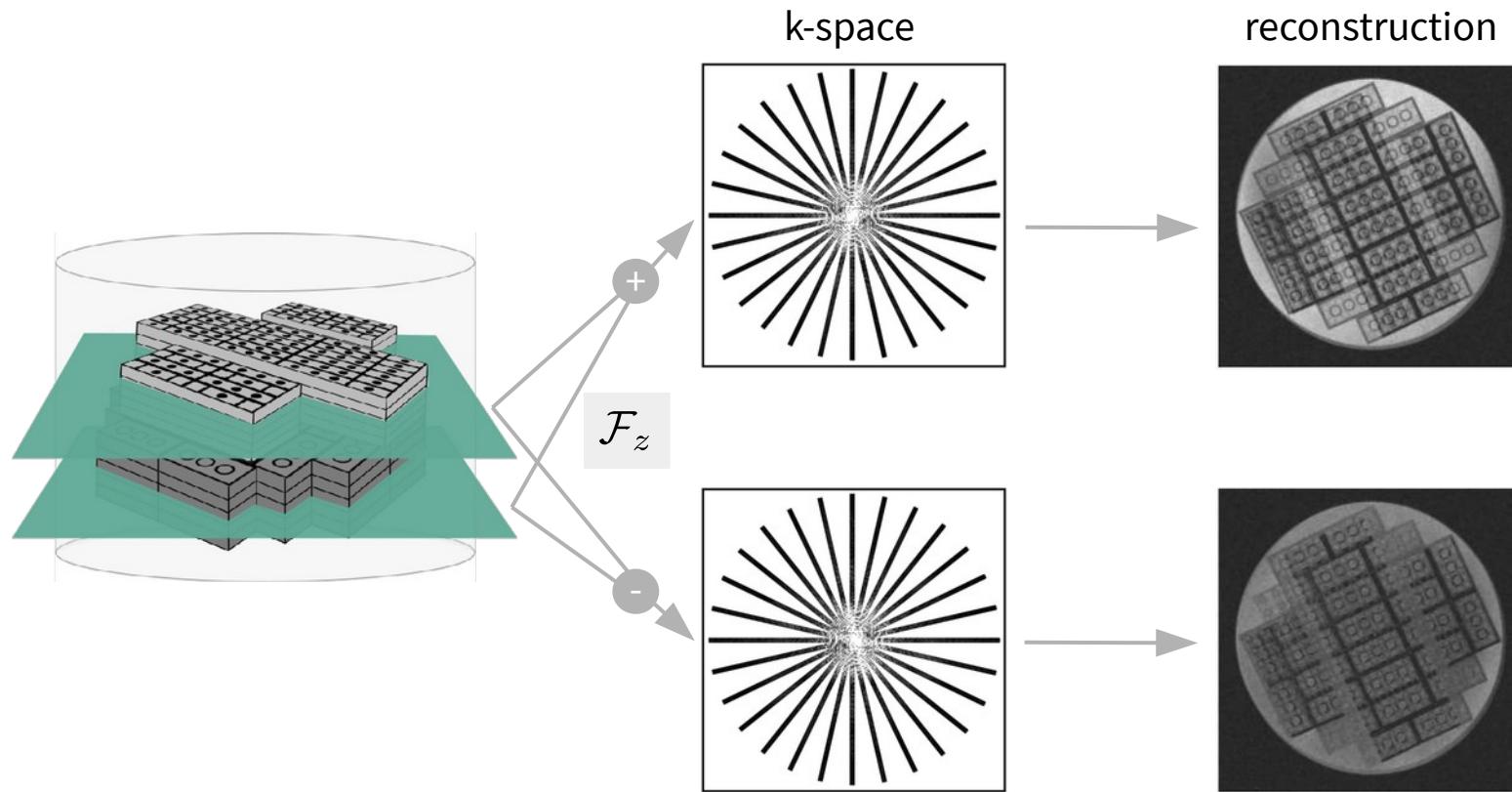
# Conventional Multi-Slice Imaging



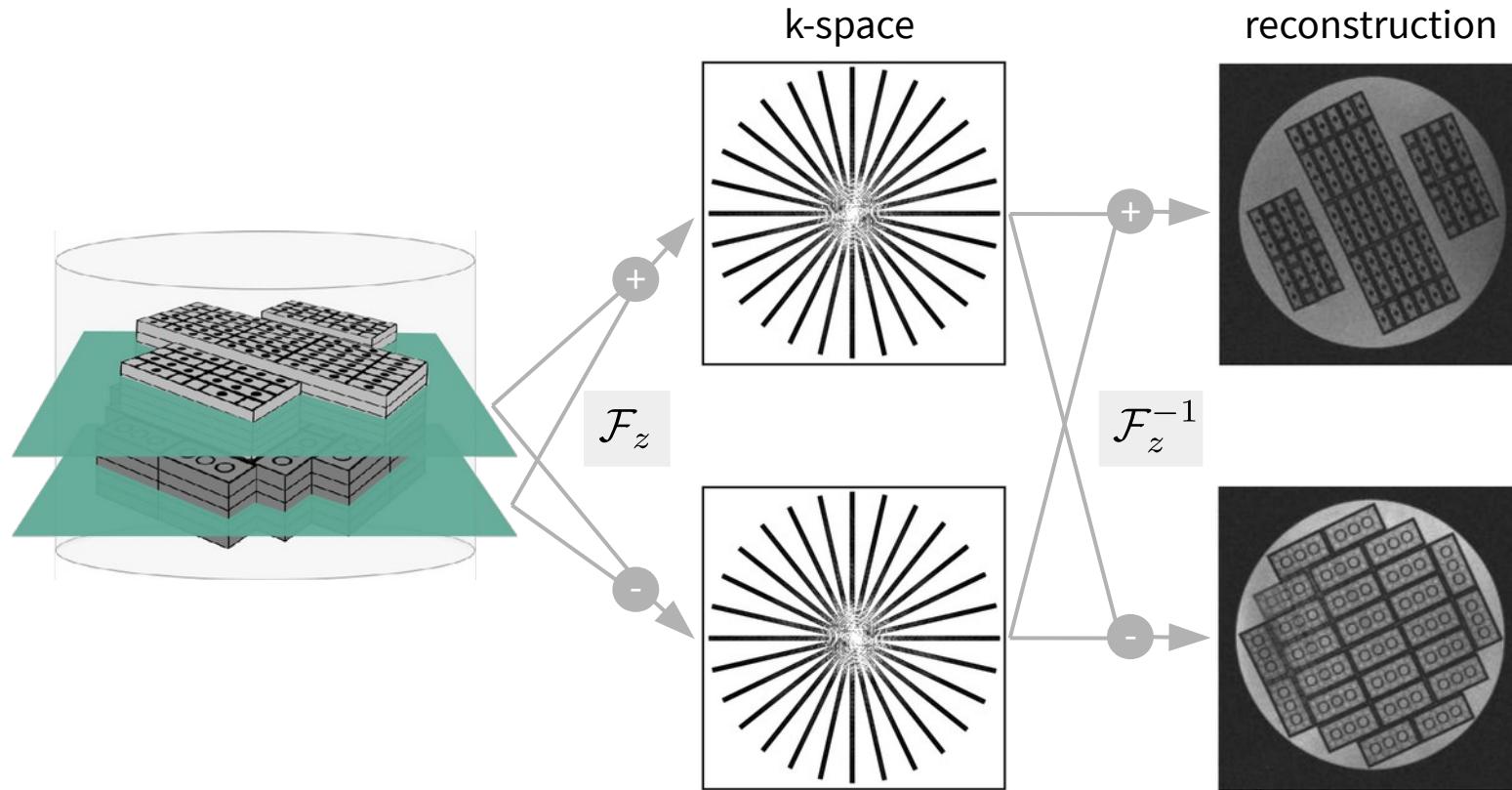
# Simultaneous Multi-Slice Imaging



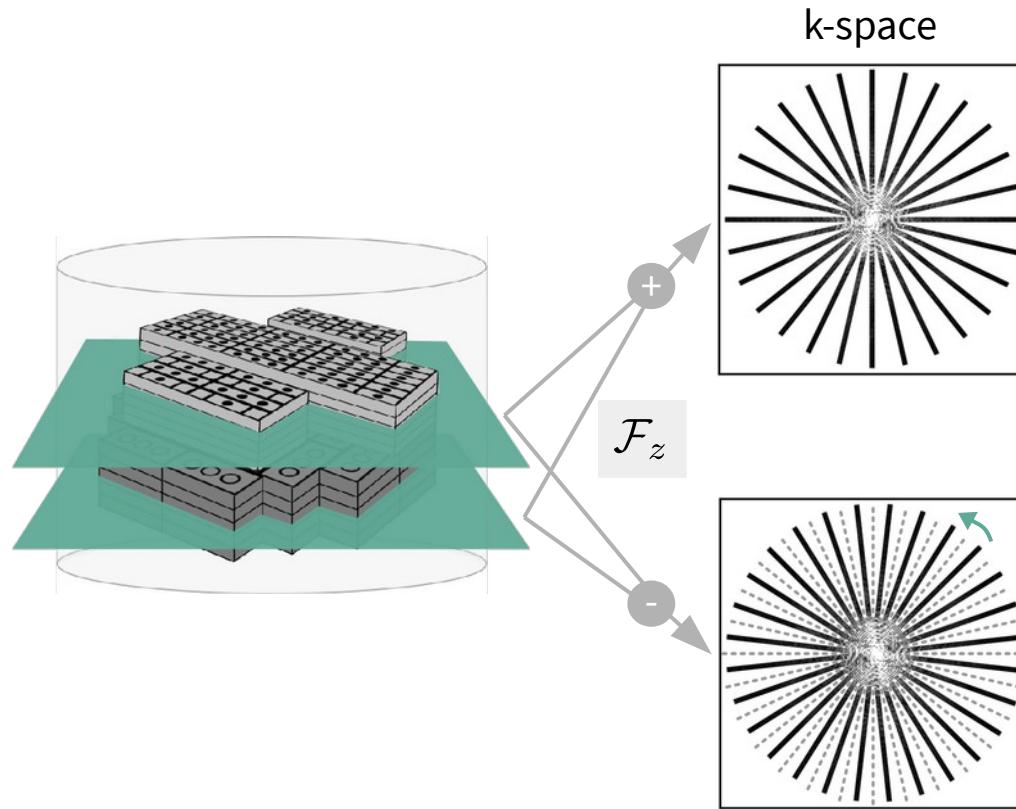
# Simultaneous Multi-Slice Imaging



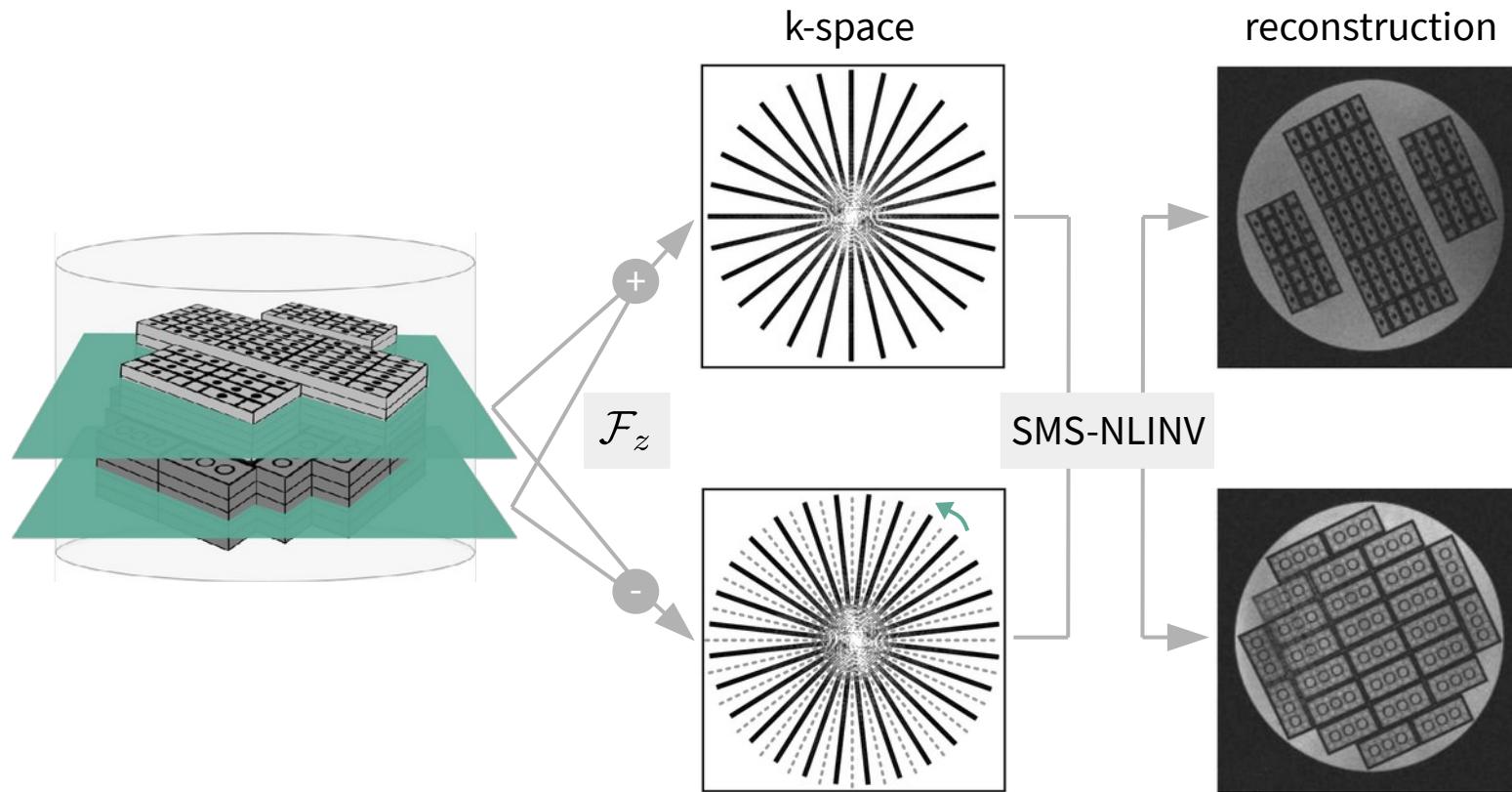
# Simultaneous Multi-Slice Imaging



# Simultaneous Multi-Slice Imaging



# Simultaneous Multi-Slice Imaging



# Optimization Problem

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$$\operatorname{argmin}_{\boldsymbol{x}} \left\| P \mathcal{F} C \boldsymbol{x} - \boldsymbol{y} \right\|^2 + R(\boldsymbol{x})$$

# Optimization Problem

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$$\operatorname{argmin}_{\boldsymbol{x}} \left\| P \mathcal{F} C \boldsymbol{x} - \boldsymbol{y} \right\|^2 + R(\boldsymbol{x})$$

$$\mathcal{F} := \mathcal{F}_{3D}$$

$$\boldsymbol{X} := (C, \boldsymbol{x})$$

$$F := P \mathcal{F}_{3D}$$

# Optimization Problem

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$$\operatorname{argmin}_{\mathbf{X}} \left| \left| F(\mathbf{X}) - \mathbf{y} \right| \right|^2 + R(\mathbf{X})$$

# Optimization Problem

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$$\operatorname{argmin}_{\mathbf{X}} \left| \left| F(\mathbf{X}) - \mathbf{y} \right| \right|^2 + R(\mathbf{X})$$

$$F(\mathbf{X}_n + d\mathbf{X}) \approx F(\mathbf{X}_n) + DF(\mathbf{X}_n)d\mathbf{X}$$

# Optimization Problem

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$$\operatorname{argmin}_{\underline{dX}} \left\| F(\mathbf{X}_n) + DF(\mathbf{X}_n) \underline{dX} - \mathbf{y} \right\|^2 + \alpha_n \left\| \mathbf{X}_n + \underline{dX} \right\|^2$$

- solve for update  $\underline{dX}$  in each Newton-step
- iterative update  $\mathbf{X}_{n+1} = \mathbf{X}_n + \underline{dX}$
- Tikhonov regularization

# Benefits

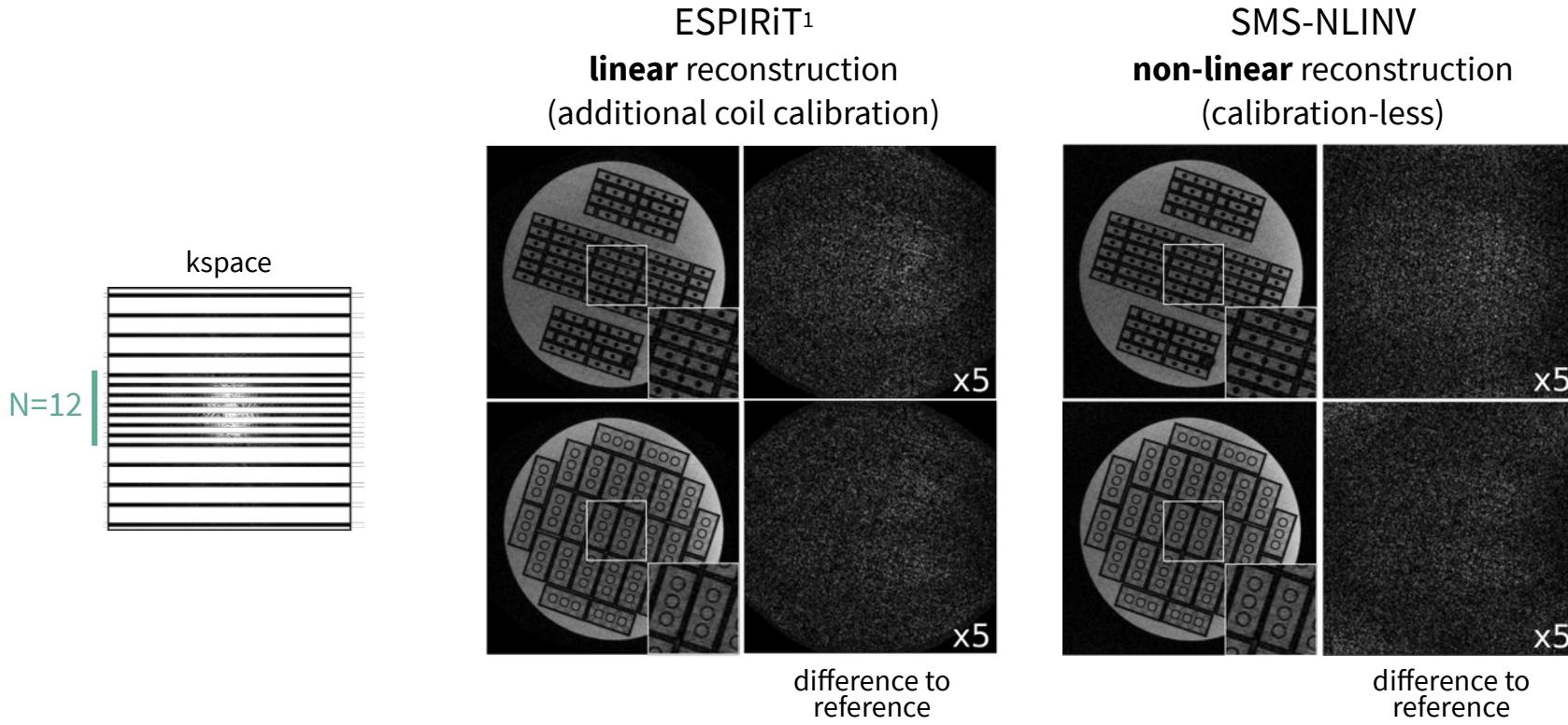
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- non-linear formulation
- complementary k-space samples



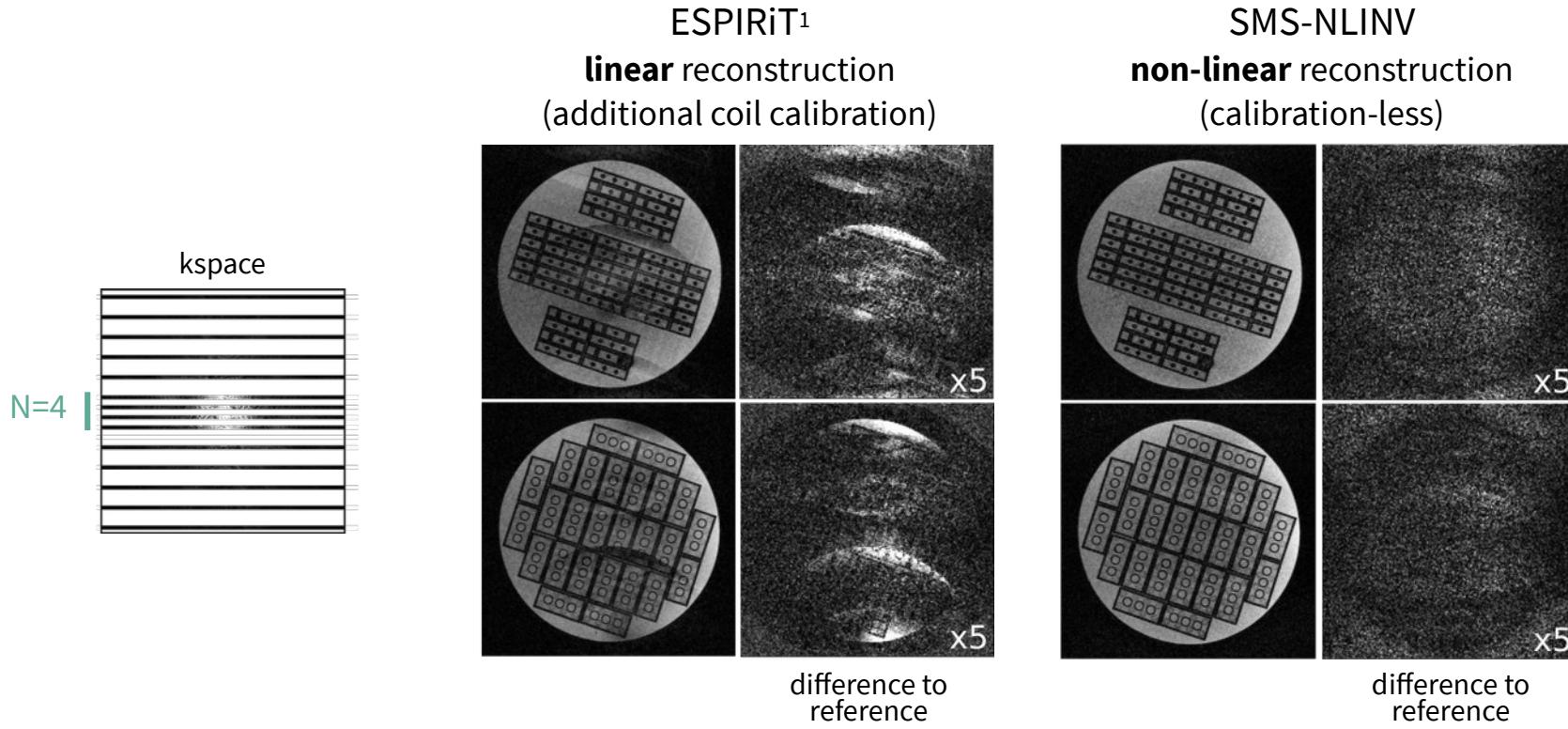
SMS-NLINV  
Cartesian | 2 slices

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SMS-NLINV  
Cartesian | 2 slices

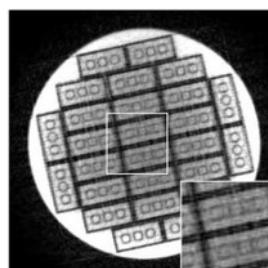
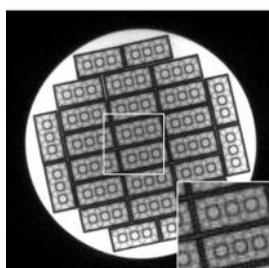
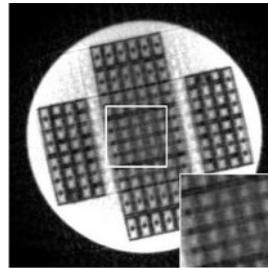
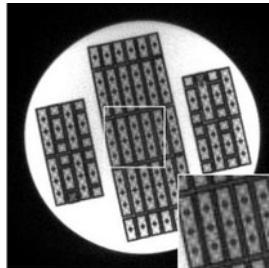
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SMS-NLINV  
Radial | 3 slices

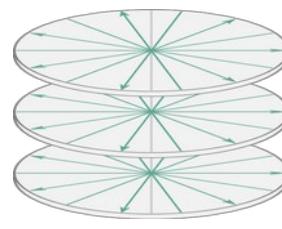
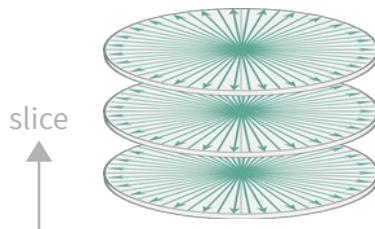
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NLINV



fully sampled

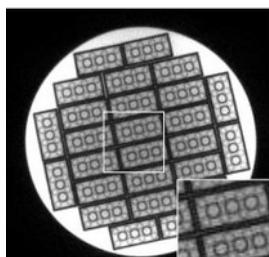
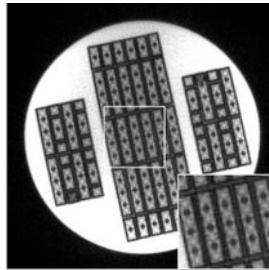
undersampled (10x)



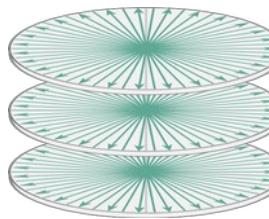
SMS-NLINV  
Radial | 3 slices

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NLINV



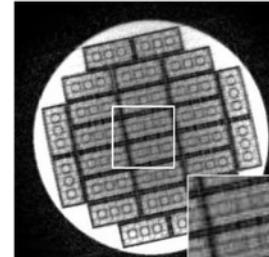
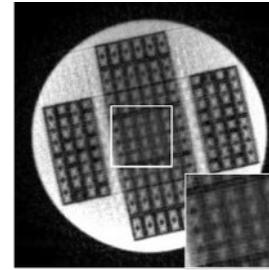
fully sampled



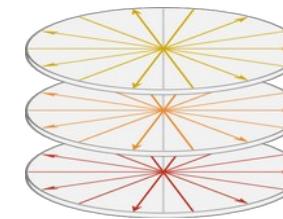
slice



SMS-NLINV



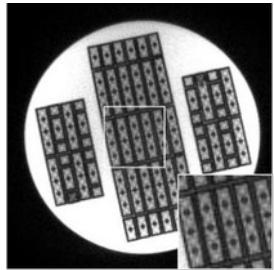
aligned (10x)



# SMS-NLINV

## Radial | 3 slices

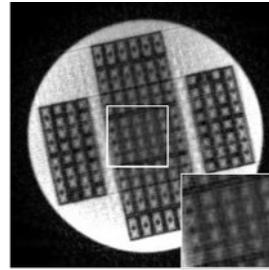
## NLINV



A grayscale image showing a circular region containing several square patterns, with a white square box highlighting one specific pattern.

A circular inset in the top right corner displays a 4x4 grid of small square plots. Each plot contains a stylized tree icon with a trunk and three leaves. The entire inset is set against a dark background.

SMS-NLINV



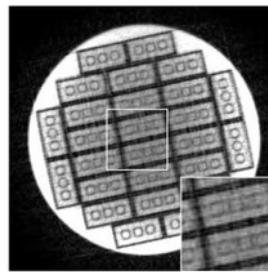
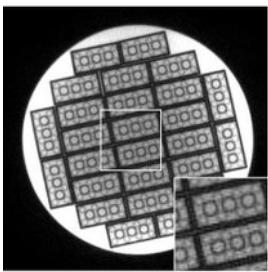
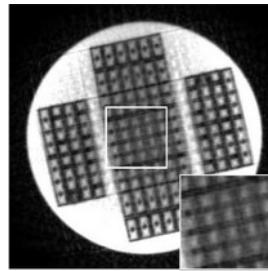
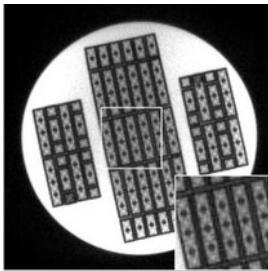
A circular inset showing a close-up view of a microfluidic device with a grid of small chambers. A white rectangular box highlights a specific area within the grid.

A circular inset showing a 4x4 grid of smaller square blocks, each containing a smaller square pattern.

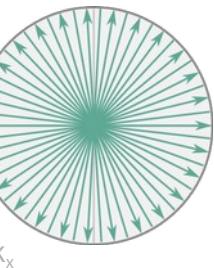
SMS-NLINV  
Radial | 3 slices

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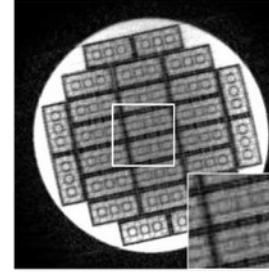
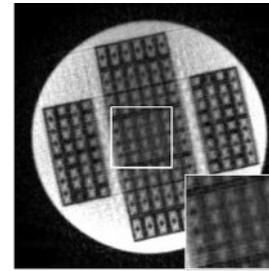
NLINV



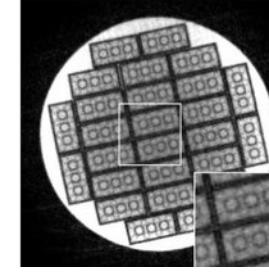
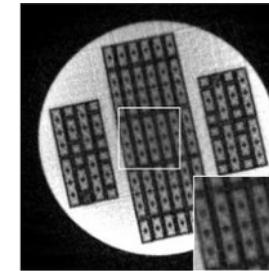
fully sampled



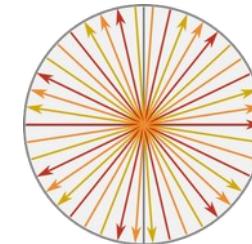
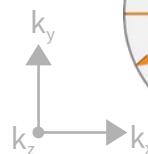
SMS-NLINV



aligned (10x)



complementary (10x)



# Temporal Regularization

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$$\underset{d\mathbf{X}^{(t)}}{\operatorname{argmin}} \|F(\mathbf{X}_n^{(t)}) + DF(\mathbf{X}_n^{(t)})d\mathbf{X}^{(t)} - \mathbf{y}\|^2 + \alpha_n \|\mathbf{X}_n^{(t)} + d\mathbf{X}^{(t)}\|^2$$

# Temporal Regularization

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$$\underset{d\mathbf{X}^{(t)}}{\operatorname{argmin}} \|F(\mathbf{X}_n^{(t)}) + DF(\mathbf{X}_n^{(t)})d\mathbf{X}^{(t)} - \mathbf{y}\|^2 + \alpha_n \|\mathbf{X}_n^{(t)} + d\mathbf{X}^{(t)}\|^2$$

# Temporal Regularization

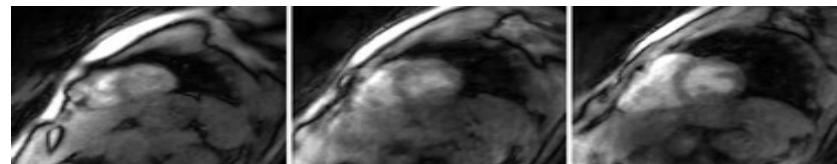
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$$\underset{d\mathbf{X}^{(t)}}{\operatorname{argmin}} \| F(\mathbf{X}_n^{(t)}) + DF(\mathbf{X}_n^{(t)}) d\mathbf{X}^{(t)} - \mathbf{y} \|^2 + \alpha_n \| \mathbf{X}_n^{(t)} + d\mathbf{X}^{(t)} - \underline{\mathbf{X}^{(t-1)}} \|^2$$

penalize the difference  
to the previous frame

SMS-NLINV  
SMS real-time MRI

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5 spokes  
*per partition & frame*

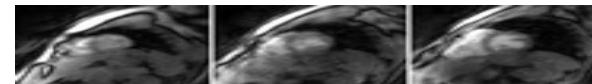
3 slices & 29 frames  
*per second*

# SMS-NLINV

## Wrap Up

### SUMMARY

- joint estimation of images and coils
  - improved image quality
  - time-consistency
  - multi-slice real-time MRI



### LIMITATIONS

- ~ 2 - 5 slices
- problem size
- SMS-FLASH study

### OUTLOOK

- SMS-bSSFP sequence
- T1 mapping<sup>1,2</sup>

SMS-NLINV T1 mapping<sup>1,2</sup>

