

NAG C Library Function Document

nag_mesh2d_join (d06dbc)

1 Purpose

nag_mesh2d_join (d06dbc) joins together (restitches) two adjacent, or overlapping, meshes.

2 Specification

```
void nag_mesh2d_join (double eps, Integer nv1, Integer nelt1, Integer nedge1,
    const double coor1[], const Integer edge1[], const Integer conn1[],
    const Integer reft1[], Integer nv2, Integer nelt2, Integer nedge2,
    const double coor2[], const Integer edge2[], const Integer conn2[],
    const Integer reft2[], Integer *nv3, Integer *nelt3, Integer *nedge3,
    double coor3[], Integer edge3[], Integer conn3[], Integer reft3[],
    Integer itrace, const char *outfile, NagError *fail)
```

3 Description

nag_mesh2d_join (d06dbc) joins together two adjacent, or overlapping, meshes. If the two meshes are adjacent then vertices belonging to the part of the boundary forming the common interface should coincide. If the two meshes overlap then vertices and triangles in the overlapping zone should coincide too.

This function is partly derived from material in the MODULEF package from INRIA (Institut National de Recherche en Informatique et Automatique).

4 References

None.

5 Parameters

- | | | |
|----|---|--------------|
| 1: | eps – double | <i>Input</i> |
| | <i>On entry:</i> the relative precision of the restitching of the two input meshes (see Section 8). | |
| | <i>Suggested value:</i> 0.001. | |
| | <i>Constraint:</i> eps > 0.0. | |
| 2: | nv1 – Integer | <i>Input</i> |
| | <i>On entry:</i> the total number of vertices in the first input mesh. | |
| | <i>Constraint:</i> nv1 ≥ 3. | |
| 3: | nelt1 – Integer | <i>Input</i> |
| | <i>On entry:</i> the number of triangular elements in the first input mesh. | |
| | <i>Constraint:</i> nelt1 ≤ 2 × nv1 – 1. | |
| 4: | nedge1 – Integer | <i>Input</i> |
| | <i>On entry:</i> the number of boundary edges in the first input mesh. | |
| | <i>Constraint:</i> nedge1 ≥ 1. | |

- 5: **coor1** $[2 \times \mathbf{nv1}]$ – const double *Input*
Note: where **COOR1**(i, j) appears in this document it refers to the array element **coor1** $[2 \times (j - 1) + i - 1]$. We recommend using a #define to make the same definition in your calling program.
On entry: **COOR1**($1, i$) contains the x -coordinate of the i th vertex of the first input mesh, for $i = 1, \dots, \mathbf{nv1}$; while **COOR1**($2, i$) contains the corresponding y -coordinate.
- 6: **edge1** $[3 \times \mathbf{nedge1}]$ – const Integer *Input*
Note: where **EDGE1**(i, j) appears in this document it refers to the array element **edge1** $[3 \times (j - 1) + i - 1]$. We recommend using a #define to make the same definition in your calling program.
On entry: the specification of the boundary edges of the first input mesh. **EDGE1**($1, j$) and **EDGE1**($2, j$) contain the vertex numbers of the two end-points of the j th boundary edge. **EDGE1**($3, j$) is a user-supplied tag for the j th boundary edge.
Constraint: $1 \leq \mathbf{EDGE1}(i, j) \leq \mathbf{nv1}$ and $\mathbf{EDGE1}(1, j) \neq \mathbf{EDGE1}(2, j)$ for $i = 1, 2$ and $j = 1, 2, \dots, \mathbf{nedge1}$.
- 7: **conn1** $[3 \times \mathbf{nelt1}]$ – const Integer *Input*
Note: where **CONN1**(i, j) appears in this document it refers to the array element **conn1** $[3 \times (j - 1) + i - 1]$. We recommend using a #define to make the same definition in your calling program.
On entry: the connectivity between triangles and vertices of the first input mesh. For each triangle j , **CONN1**(i, j) gives the indices of its three vertices (in anticlockwise order), for $i = 1, 2, 3$ and $j = 1, \dots, \mathbf{nelt1}$.
Constraints:
 $1 \leq \mathbf{CONN1}(i, j) \leq \mathbf{nv1}$;
 $\mathbf{CONN1}(1, j) \neq \mathbf{CONN1}(2, j)$;
 $\mathbf{CONN1}(1, j) \neq \mathbf{CONN1}(3, j)$ and $\mathbf{CONN1}(2, j) \neq \mathbf{CONN1}(3, j)$ for $i = 1, 2, 3$ and $j = 1, 2, \dots, \mathbf{nelt1}$.
- 8: **reft1** $[\mathbf{nelt1}]$ – const Integer *Input*
On entry: **reft1** $[k - 1]$ contains the user-supplied tag of the k th triangle from the first input mesh, for $k = 1, \dots, \mathbf{nelt1}$.
- 9: **nv2** – Integer *Input*
On entry: the total number of vertices in the second input mesh.
Constraint: $\mathbf{nv2} \geq 3$.
- 10: **nelt2** – Integer *Input*
On entry: the number of triangular elements in the second input mesh.
Constraint: $\mathbf{nelt2} \leq 2 \times \mathbf{nv2} - 1$.
- 11: **nedge2** – Integer *Input*
On entry: the number of boundary edges in the second input mesh.
Constraint: $\mathbf{nedge2} \geq 1$.
- 12: **coor2** $[2 \times \mathbf{nv2}]$ – const double *Input*
Note: where **COOR2**(i, j) appears in this document it refers to the array element **coor2** $[2 \times (j - 1) + i - 1]$. We recommend using a #define to make the same definition in your calling program.

On entry: **COOR2**(1, i) contains the x -coordinate of the i th vertex of the second input mesh, for $i = 1, \dots, \mathbf{nv2}$; while **COOR2**(2, i) contains the corresponding y -coordinate.

13: **edge2**[$3 \times \mathbf{nedge2}$] – const Integer *Input*

Note: where **EDGE2**(i, j) appears in this document it refers to the array element **edge2**[$3 \times (j - 1) + i - 1$]. We recommend using a #define to make the same definition in your calling program.

On entry: the specification of the boundary edges of the second input mesh. **EDGE2**(1, j) and **EDGE2**(2, j) contain the vertex numbers of the two end-points of the j th boundary edge. **EDGE2**(3, j) is a user-supplied tag for the j th boundary edge.

Constraint: $1 \leq \mathbf{EDGE2}(i, j) \leq \mathbf{nv2}$ and $\mathbf{EDGE2}(1, j) \neq \mathbf{EDGE2}(2, j)$ for $i = 1, 2$ and $j = 1, 2, \dots, \mathbf{nedge2}$.

14: **conn2**[$3 \times \mathbf{nelt2}$] – const Integer *Input*

Note: where **CONN2**(i, j) appears in this document it refers to the array element **conn2**[$3 \times (j - 1) + i - 1$]. We recommend using a #define to make the same definition in your calling program.

On entry: the connectivity between triangles and vertices of the second input mesh. For each triangle j , **CONN2**(i, j) gives the indices of its three vertices (in anticlockwise order), for $i = 1, 2, 3$ and $j = 1, \dots, \mathbf{nelt2}$.

Constraints:

$1 \leq \mathbf{CONN2}(i, j) \leq \mathbf{nv2}$;
 $\mathbf{CONN2}(1, j) \neq \mathbf{CONN2}(2, j)$;
 $\mathbf{CONN2}(1, j) \neq \mathbf{CONN2}(3, j)$ and $\mathbf{CONN2}(2, j) \neq \mathbf{CONN2}(3, j)$ for $i = 1, 2, 3$ and $j = 1, 2, \dots, \mathbf{nelt2}$.

15: **reft2**[$\mathbf{nelt2}$] – const Integer *Input*

On entry: **reft2**[$k - 1$] contains the user-supplied tag of the k th triangle from the second input mesh, for $k = 1, \dots, \mathbf{nelt2}$.

16: **nv3** – Integer * *Output*

On exit: the total number of vertices in the resulting mesh.

17: **nelt3** – Integer * *Output*

On exit: the number of triangular elements in the resulting mesh.

18: **nedge3** – Integer * *Output*

On exit: the number of boundary edges in the resulting mesh.

19: **coor3**[$\mathbf{dim}$] – double *Output*

Note: where **COOR3**(i, j) appears in this document it refers to the array element **coor3**[$2 \times (j - 1) + i - 1$]. We recommend using a #define to make the same definition in your calling program.

The dimension, $\mathbf{dim}$, of the array **coor3** must be at least $2 \times (\mathbf{nv1} + \mathbf{nv2})$. This may be reduced to **nv3** once that value is known.

On exit: **COOR3**(1, i) will contain the x -coordinate of the i th vertex of the resulting mesh, for $i = 1, \dots, \mathbf{nv3}$; while **COOR3**(2, i) will contain the corresponding y -coordinate.

20: **edge3**[$\mathbf{dim}$] – Integer *Output*

Note: where **EDGE3**(i, j) appears in this document it refers to the array element **edge3**[$3 \times (j - 1) + i - 1$]. We recommend using a #define to make the same definition in your calling program.

The dimension, dim , of the array **edge3** must be at least $3 \times (\mathbf{nedge1} + \mathbf{nedge2})$. This may be reduced to **nedge3** once that value is known.

On exit: the specification of the boundary edges of the resulting mesh. **EDGE3**(i, j) will contain the vertex number of the i th end-point ($i = 1, 2$) of the j th boundary or interface edge.

If the two meshes overlap, **EDGE3**($3, j$) will contain the same tag as the corresponding edge belonging to the first and/or the second input mesh.

If the two meshes are adjacent,

- (i) if the j th edge is part of the partition interface, then **EDGE3**($3, j$) will contain the value $1000 \times k_1 + k_2$ where k_1 and k_2 are the tags for the same edge of the first and the second mesh respectively;
- (ii) otherwise, **EDGE3**($3, j$) will contain the same tag as the corresponding edge belonging to the first and/or the second input mesh.

21: **conn3**[dim] – Integer *Output*

Note: where **CONN3**(i, j) appears in this document it refers to the array element **conn3**[$3 \times (j - 1) + i - 1$]. We recommend using a #define to make the same definition in your calling program.

The dimension, dim , of the array **conn3** must be at least $3 \times (\mathbf{nelt1} + \mathbf{nelt2})$. This may be reduced to **nelt3** once that value is known.

On exit: the connectivity between triangles and vertices of the resulting mesh. **CONN3**(i, j) will give the indices of its three vertices (in anticlockwise order), for $i = 1, 2, 3$ and $j = 1, \dots, \mathbf{nelt3}$.

22: **reft3**[dim] – Integer *Output*

Note: the dimension, dim , of the array **reft3** must be at least **nelt1** + **nelt2**. This may be reduced to **nelt3** once that value is known.

On exit: if the two meshes form a partition, **reft3**[$k - 1$] will contain the same tag as the corresponding triangle belonging to the first or the second input mesh, for $k = 1, \dots, \mathbf{nelt3}$. If the two meshes overlap, then **reft3**[$k - 1$] will contain the value $1000 \times k_1 + k_2$ where k_1 and k_2 are the user-supplied tags for the same triangle of the first and the second mesh respectively, for $k = 1, \dots, \mathbf{nelt3}$.

23: **itrace** – Integer *Input*

On entry: the level of trace information required from nag_mesh2d_join (d06dbc) as follows:

if **itrace** ≤ 0 , no output is generated;

if **itrace** ≥ 1 , then details about the common vertices, edges and triangles to both meshes are printed.

24: **outfile** – char * *Input*

On entry: the name of a file to which diagnostic output will be directed. If **outfile** is NULL the diagnostic output will be directed to standard output.

25: **fail** – NagError * *Input/Output*

The NAG error parameter (see the Essential Introduction).

6 Error Indicators and Warnings

NE_INT

On entry, **nv1** = $\langle value \rangle$.

Constraint: **nv1** ≥ 3 .

On entry, **nedge1** = $\langle value \rangle$.

Constraint: **nedge1** ≥ 1 .

On entry, **nv2** = $\langle value \rangle$.

Constraint: **nv2** ≥ 3 .

On entry, **nedge2** = $\langle value \rangle$.

Constraint: **nedge2** ≥ 1 .

NE_INT_2

On entry, the endpoints of edge j in the 2nd mesh have the same index i : $j = \langle value \rangle$, $i = \langle value \rangle$.

On entry, vertices 2 and 3 of triangle k in the 2nd mesh have the same index i : $k = \langle value \rangle$, $i = \langle value \rangle$.

On entry, **nelt1** $> (2 \times \mathbf{nv1} - 1)$: **nelt1** = $\langle value \rangle$, **nv1** = $\langle value \rangle$.

On entry, vertices 1 and 3 of triangle k in the 2nd mesh have the same index i : $k = \langle value \rangle$, $i = \langle value \rangle$.

On entry, vertices 1 and 2 of triangle k in the 2nd mesh have the same index i : $k = \langle value \rangle$, $i = \langle value \rangle$.

On entry, the endpoints of edge j in the 1st mesh have the same index i : $j = \langle value \rangle$, $i = \langle value \rangle$.

On entry, vertices 2 and 3 of triangle k in the 1st mesh have the same index i : $k = \langle value \rangle$, $i = \langle value \rangle$.

On entry, **nelt2** $> (2 \times \mathbf{nv2} - 1)$: **nelt2** = $\langle value \rangle$, **nv2** = $\langle value \rangle$.

On entry, vertices 1 and 3 of triangle k in the 1st mesh have the same index i : $k = \langle value \rangle$, $i = \langle value \rangle$.

On entry, vertices 1 and 2 of triangle k in the 1st mesh have the same index i : $k = \langle value \rangle$, $i = \langle value \rangle$.

NE_INT_4

On entry, **conn2**(i, j) < 1 or **conn2**(i, j) $> \mathbf{nv2}$, where **conn2**(i, j) denotes **conn2**[$3 \times (j - 1) + i - 1$]: **conn2**(i, j) = $\langle value \rangle$, $i = \langle value \rangle$, $j = \langle value \rangle$, **nv2** = $\langle value \rangle$.

On entry, **edge1**(i, j) < 1 or **edge1**(i, j) $> \mathbf{nv1}$, where **edge1**(i, j) denotes **edge1**[$3 \times (j - 1) + i - 1$]: **edge1**(i, j) = $\langle value \rangle$, $i = \langle value \rangle$, $j = \langle value \rangle$, **nv1** = $\langle value \rangle$.

On entry, **conn1**(i, j) < 1 or **conn1**(i, j) $> \mathbf{nv1}$, where **conn1**(i, j) denotes **conn1**[$3 \times (j - 1) + i - 1$]: **conn1**(i, j) = $\langle value \rangle$, $i = \langle value \rangle$, $j = \langle value \rangle$, **nv1** = $\langle value \rangle$.

On entry, **edge2**(i, j) < 1 or **edge2**(i, j) $> \mathbf{nv2}$, where **edge2**(i, j) denotes **edge2**[$3 \times (j - 1) + i - 1$]: **edge2**(i, j) = $\langle value \rangle$, $i = \langle value \rangle$, $j = \langle value \rangle$, **nv2** = $\langle value \rangle$.

NE_MESH_ERROR

The routine has detected a different number of coincident triangles from the two meshes in the overlapping zone $\langle value \rangle$ $\langle value \rangle$. Check the input of the two meshes, especially the triangles/vertices connectivity.

The routine has detected a different number of coincident edges from the two meshes on the partition interface $\langle value \rangle$ $\langle value \rangle$. Check the input of the two meshes, especially the edges/vertices connectivity.

The routine has detected only $\langle value \rangle$ coincident vertices with a precision **eps** = $\langle value \rangle$. Either **eps** should be changed or the two meshes are not restitchable.

A serious error has occurred in an internal call to the restitching routine. Check the input of the two meshes, especially the edges/vertices and/or the triangles/vertices connectivities. Seek expert help.

NE_REAL

On entry, **eps** = $\langle value \rangle$.
 Constraint: **eps** > 0.0.

NE_ALLOC_FAIL

Memory allocation failed.

NE_BAD_PARAM

On entry, parameter $\langle value \rangle$ had an illegal value.

NE_NOT_WRITE_FILE

Cannot open file $\langle value \rangle$ for writing.

NE_NOT_CLOSE_FILE

Cannot close file $\langle value \rangle$.

NE_INTERNAL_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please consult NAG for assistance.

7 Accuracy

Not applicable.

8 Further Comments

nag_mesh2d_join (d06dbc) finds all the common vertices between the two input meshes using the relative precision of the restitching parameter **eps**. The user is advised to vary the value of **eps** in the neighborhood of 0.001 with **itrace** ≥ 1 to get the optimal value for the meshes under consideration.

9 Example

For this function two examples are presented. There is a single example program for nag_mesh2d_join (d06dbc), with a main program and the code to solve the two example problems is given in the functions *ex1* and *ex2* respectively.

```
/* nag_mesh2d_join (d06dbc) Example Program.
 *
 * Copyright 2001 Numerical Algorithms Group.
 *
 * Mark 7, 2001.
 */

#include <stdio.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagd06.h>

static double fbnd(Integer , double , double , Nag_Comm *);

extern int ex1(void), ex2(void);

#define EDGE1(I,J) edge1[3*((J)-1)+(I)-1]
#define EDGE2(I,J) edge2[3*((J)-1)+(I)-1]
#define EDGE3(I,J) edge3[3*((J)-1)+(I)-1]
#define EDGE4(I,J) edge4[3*((J)-1)+(I)-1]
#define EDGE5(I,J) edge5[3*((J)-1)+(I)-1]
#define CONN1(I,J) conn1[3*((J)-1)+(I)-1]
#define CONN2(I,J) conn2[3*((J)-1)+(I)-1]
```

```

#define CONN3(I,J) conn3[3*((J)-1)+(I)-1]
#define CONN4(I,J) conn4[3*((J)-1)+(I)-1]
#define CONN5(I,J) conn5[3*((J)-1)+(I)-1]
#define COOR1(I,J) coor1[2*((J)-1)+(I)-1]
#define COOR2(I,J) coor2[2*((J)-1)+(I)-1]
#define COOR3(I,J) coor3[2*((J)-1)+(I)-1]
#define COOR4(I,J) coor4[2*((J)-1)+(I)-1]
#define COOR5(I,J) coor5[2*((J)-1)+(I)-1]
#define TRANS(I,J) trans[6*((J)-1)+(I)-1]
#define LINED(I,J) lined[4*((J)-1)+(I)-1]
#define COORCH(I,J) coorch[2*(J-1)+I-1]
#define COORUS(I,J) coorus[2*(J-1)+I-1]

int main(void)
{
    Vprintf("d06dbc Example Program Results\n");

    ex1();
    ex2();

    return 0;
}

int ex1(void)
{
    const Integer nvmax=900, nedmx=200, neltmx=2*nvmax+5, ntrans=1, mode=0;
    double eps;
    Integer exit_status, i, imax, itrace, itrans, jmax, jtrans, k, ktrans,
        nedgel, nedge2, nedge3, nelt1, nelt2, nelt3, nv1, nv2, nv3, reftk;
    Integer imaxml, jmaxml, ind;
    char pmesh[2];
    double *coor1=0, *coor2=0, *coor3=0, *trans=0;
    Integer *conn1=0, *conn2=0, *conn3=0, *edgel=0,
        *edge2=0, *edge3=0, *itype=0, *reft1=0, *reft2=0, *reft3=0;
    NagError fail;

    INIT_FAIL(fail);
    exit_status = 0;

    Vprintf("\nExample 1\n\n");

    /* Skip heading in data file */

    Vscanf("%*[^\\n] ");
    Vscanf("%*[^\\n] ");

    /* Read the mesh: coordinates and connectivity of the 1st domain */

    Vscanf("%ld", &nv1);
    Vscanf("%ld", &nelt1);
    Vscanf("%*[^\\n] ");

    nv2 = nv1;
    nelt2 = nelt1;

    imax = 20;
    jmax = imax;
    imaxml = imax - 1;
    jmaxml = jmax - 1;
    nedgel = 2*(imaxml + jmaxml);
    nedge2 = nedgel;

    /* Allocate memory */

    if ( !(coor1 = NAG_ALLOC(2*nv1, double)) ||
        !(coor2 = NAG_ALLOC(2*nv2, double)) ||
        !(coor3 = NAG_ALLOC(2*nvmax, double)) ||
        !(trans = NAG_ALLOC(6*ntrans, double)) ||
        !(conn1 = NAG_ALLOC(3*nelt1, Integer)) ||
        !(conn2 = NAG_ALLOC(3*nelt2, Integer)) ||
        !(conn3 = NAG_ALLOC(3*neltmx, Integer)) ||

```

```

        !(edge1 = NAG_ALLOC(3*nedge1, Integer)) ||
        !(edge2 = NAG_ALLOC(3*nedge2, Integer)) ||
        !(edge3 = NAG_ALLOC(3*nedmx, Integer)) ||
        !(itype = NAG_ALLOC(ntrans, Integer)) ||
        !(reft1 = NAG_ALLOC(nelt1, Integer)) ||
        !(reft2 = NAG_ALLOC(nelt2, Integer)) ||
        !(reft3 = NAG_ALLOC(neltmx, Integer)) )
    {
        Vprintf("Allocation failure\n");
        exit_status = -1;
        goto END;
    }

    for (i = 1; i <= nv1; ++i)
    {
        Vscanf("%lf", &COOR1(1,i));
        Vscanf("%lf", &COOR1(2,i));
        Vscanf("%*[\n] ");
    }

    for (k = 1; k <= nelt1; ++k)
    {
        Vscanf("%ld", &CONN1(1,k));
        Vscanf("%ld", &CONN1(2,k));
        Vscanf("%ld", &CONN1(3,k));
        Vscanf("%ld", &reftk);
        Vscanf("%*[\n] ");

        reft1[k-1] = 1;
        reft2[k-1] = 2;
    }

    Vscanf(" ' %1s '", pmesh);
    Vscanf("%*[\n] ");

    /* the edges of the boundary */

    ind = 0;

    for (i = 1; i <= imaxm1; ++i)
    {
        ++ind;
        EDGE1(1,ind) = i;
        EDGE1(2,ind) = i + 1;
        EDGE1(3,ind) = 1;
    }

    for (i = 1; i <= jmaxm1; ++i)
    {
        ++ind;
        EDGE1(1,ind) = i*imax;
        EDGE1(2,ind) = (i+1)*imax;
        EDGE1(3,ind) = 1;
    }

    for (i = 1; i <= imaxm1; ++i)
    {
        ++ind;
        EDGE1(1,ind) = imax*jmax - i + 1;
        EDGE1(2,ind) = imax*jmax - i;
        EDGE1(3,ind) = 1;
    }

    for (i = 1; i <= jmaxm1; ++i)
    {
        ++ind;
        EDGE1(1,ind) = (jmax - i)*imax + 1;
        EDGE1(2,ind) = (jmax - i - 1)*imax + 1;
        EDGE1(3,ind) = 1;
    }

```



```

for (ktrans = 0; ktrans < 2; ++ktrans)
{
    /* Translation of the 1st domain to obtain the 2nd domain */
    /* KTRANS = 0 leading to a domain overlapping */
    /* KTRANS = 1 leading to a domain partition */

    if (ktrans == 0)
    {
        itrans = imax - 5;
        jtrans = jmax - 3;
    }
    else
    {
        itrans = imax - 1;
        jtrans = 0;
    }

    itype[0] = 1;
    TRANS(1, 1) = (double)itrans/(imax - 1.0);
    TRANS(2, 1) = (double)jtrans/(jmax - 1.0);
    itrace = 0;

    d06dac(mode, nv2, nedge2, nelt2, ntrans, itype, trans, coor1,
           edge1, conn1, coor2, edge2, conn2, itrace, 0, &fail);

    if (fail.code == NE_NOERROR)
    {
        for (i = 1; i <= nedge2; ++i) EDGE2(3, i) = 2;

        /* Call to the restitching driver */

        itrace = 0;
        eps = 0.01;

        d06dbc(eps, nv1, nelt1, nedge1, coor1, edge1, conn1, reft1,
              nv2, nelt2, nedge2, coor2, edge2, conn2, reft2, &nv3,
              &nelt3, &nedge3, coor3, edge3, conn3, reft3, itrace,
              0, &fail);

        if (fail.code == NE_NOERROR)
        {
            if (pmesh[0] == 'N')
            {
                if (ktrans == 0)
                {
                    Vprintf("The restitched mesh characteristics\n");
                    Vprintf("in the overlapping case\n");
                }
                else
                {
                    Vprintf("in the partition case\n");
                }
                Vprintf(" nv      =%6ld\n", nv3);
                Vprintf(" nelt   =%6ld\n", nelt3);
                Vprintf(" nedge =%6ld\n", nedge3);
            }
            else if (pmesh[0] == 'Y')
            {
                /* Output the mesh to view it using the
                 NAG Graphics Library */

                Vprintf(" %10ld%10ld%10ld\n", nv3, nelt3, nedge3);

                for (i = 1; i <= nv3; ++i)
                    Vprintf("  %12.6e %12.6e\n",
                           COOR3(1,i), COOR3(2,i));

                for (k = 1; k <= nelt3; ++k)
                    Vprintf(" %10ld%10ld%10ld%10ld\n",
                           CONN3(1,k), CONN3(2,k), CONN3(3,k), reft3[k - 1]);
            }
        }
    }
}

```

```

        for (k = 1; k <= nedge3; ++k)
            Vprintf(" %10ld%10ld%10ld\n",
                    EDGE3(1,k), EDGE3(2,k), EDGE3(3,k));
    }
    else
    {
        Vprintf("Problem with the printing option Y or N\n");
        exit_status = -1;
        goto END;
    }
}
else
{
    Vprintf("Error from d06dbc.\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}
}
else
{
    Vprintf("Error from d06dac.\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}
}

END:

if (coor1) NAG_FREE(coor1);
if (coor2) NAG_FREE(coor2);
if (coor3) NAG_FREE(coor3);
if (trans) NAG_FREE(trans);
if (conn1) NAG_FREE(conn1);
if (conn2) NAG_FREE(conn2);
if (conn3) NAG_FREE(conn3);
if (edge1) NAG_FREE(edge1);
if (edge2) NAG_FREE(edge2);
if (edge3) NAG_FREE(edge3);
if (itype) NAG_FREE(itype);
if (reft1) NAG_FREE(reft1);
if (reft2) NAG_FREE(reft2);
if (reft3) NAG_FREE(reft3);

return exit_status;
}

int ex2(void)
{
    const Integer nvmax=900, nedmx=200, neltnx=2*nvmax+5,
        ntrans=1, nus=0, nvint=0, nvfix=0;
    double eps;
    Integer exit_status, i, itrace, j, k, l, ncomp, nedge1,
        nedge2, nedge3, nedge4, nedge5, nelt1, nelt2, nelt3,
        nelt4, nelt5, nlines, npropa, nqint, nv1, nv2, nv3, nv4,
        nv5, nvb1, nvb2, mode;
    char pmesh[2];
    double *coor1=0, *coor2=0, *coor3=0, *coor4=0, *coor5=0,
        *coorch=0, *coorus=0, *rate=0, *trans=0, *weight=0;
    Integer *conn1=0, *conn2=0, *conn3=0, *conn4=0, *conn5=0,
        *edge1=0, *edge2=0, *edge3=0, *edge4=0, *edge5=0, *itype=0,
        *lcomp=0, *lined=0, *nlcomp=0, *numfix=0, *reft1=0, *reft2=0,
        *reft3=0, *reft4=0, *reft5=0;
    NagError fail;
    Nag_Comm comm;

    INIT_FAIL(fail);
    exit_status = 0;

    Vprintf("\nExample 2\n\n");

```

```

/* Skip heading in data file */

Vscanf("%*[\n] ");

/* Build the mesh of the 1st domain */
/* Initialise boundary mesh inputs: */
/* the number of line and of the characteristic points of */
/* the boundary mesh */

Vscanf("%ld", &nlines);
Vscanf("%*[\n] ");

/* Allocate memory */

if ( !(coor1 = NAG_ALLOC(2*nvmax, double)) ||
      !(coor2 = NAG_ALLOC(2*nvmax, double)) ||
      !(coor3 = NAG_ALLOC(2*nvmax, double)) ||
      !(coor4 = NAG_ALLOC(2*nvmax, double)) ||
      !(coor5 = NAG_ALLOC(2*nvmax, double)) ||
      !(coorch = NAG_ALLOC(2*nlines, double)) ||
      !(coorus = NAG_ALLOC(1, double)) ||
      !(rate = NAG_ALLOC(nlines, double)) ||
      !(trans = NAG_ALLOC(6*ntrans, double)) ||
      !(weight = NAG_ALLOC(1, double)) ||
      !(conn1 = NAG_ALLOC(3*neltmx, Integer)) ||
      !(conn2 = NAG_ALLOC(3*neltmx, Integer)) ||
      !(conn3 = NAG_ALLOC(3*neltmx, Integer)) ||
      !(conn4 = NAG_ALLOC(3*neltmx, Integer)) ||
      !(conn5 = NAG_ALLOC(3*neltmx, Integer)) ||
      !(edge1 = NAG_ALLOC(3*nedmx, Integer)) ||
      !(edge2 = NAG_ALLOC(3*nedmx, Integer)) ||
      !(edge3 = NAG_ALLOC(3*nedmx, Integer)) ||
      !(edge4 = NAG_ALLOC(3*nedmx, Integer)) ||
      !(edge5 = NAG_ALLOC(3*nedmx, Integer)) ||
      !(itype = NAG_ALLOC(ntrans, Integer)) ||
      !(lcomp = NAG_ALLOC(nlines, Integer)) ||
      !(lined = NAG_ALLOC(4*nlines, Integer)) ||
      !(numfix = NAG_ALLOC(1, Integer)) ||
      !(ref1 = NAG_ALLOC(2*nvmax+5, Integer)) ||
      !(ref2 = NAG_ALLOC(2*nvmax+5, Integer)) ||
      !(ref3 = NAG_ALLOC(2*nvmax+5, Integer)) ||
      !(ref4 = NAG_ALLOC(2*nvmax+5, Integer)) ||
      !(ref5 = NAG_ALLOC(2*nvmax+5, Integer)) )
{
    Vprintf("Allocation failure\n");
    exit_status = -1;
    goto END;
}

/* Characteristic points of the boundary geometry */

for (j = 1; j <= nlines; ++j)
{
    Vscanf("%lf", &COORCH(1,j));
}
Vscanf("%*[\n] ");

for (j = 1; j <= nlines; ++j)
{
    Vscanf("%lf", &COORCH(2,j));
}
Vscanf("%*[\n] ");

/* The lines of the boundary mesh */

for (j = 1; j <= nlines; ++j)
{
    for (i = 1; i <= 4; ++i) Vscanf("%ld", &LINED(i,j));
    Vscanf("%lf", &rate[j - 1]);
}
Vscanf("%*[\n] ");

```

```

/* The number of connected components */
/* on the boundary and their data */

Vscanf("%ld", &ncomp);
Vscanf("%*[^\\n] ");

/* Allocate memory */

if ( !(nlcomp = NAG_ALLOC(ncomp, Integer)) )
{
    Vprintf("Allocation failure\\n");
    exit_status = -1;
    goto END;
}

j = 1;

for (i = 1; i <= ncomp; ++i)
{
    Vscanf("%ld", &nlcomp[i - 1]);
    Vscanf("%*[^\\n] ");
    l = j + abs(nlcomp[i - 1]) - 1;
    for (k = j; k <= l; ++k) Vscanf("%ld", &lcomp[k - 1]);
    Vscanf("%*[^\\n] ");
    j += abs(nlcomp[i - 1]);
}

itrace = 0;

/* Call to the 2D boundary mesh generator */

d06bac(nlines, coorch, lined, fbnd, coorus, nus, rate, ncomp,
        nlcomp, lcomp, nvmax, nedmx, &nvbl, coor1, &nedge1,
        edge1, itrace, 0, &comm, &fail);

if (fail.code != NE_NOERROR)
{
    Vprintf("Error from d06bac.\\n%s\\n", fail.message);
    exit_status = 1;
    goto END;
}

/* Generate mesh using Delaunay-Voronoi method */

/* Initialise mesh control parameters */

itrace = 0;
npropa = 1;

d06abc(nvbl, nvint, nvmax, nedge1, edge1, &nv1, &nelt1, coor1,
        conn1, weight, npropa, itrace, 0, &fail);

if (fail.code != NE_NOERROR)
{
    Vprintf("Error from d06abc.\\n%s\\n", fail.message);
    exit_status = 1;
    goto END;
}

for (k = 1; k <= nelt1; ++k) reft1[k - 1] = 1;

/* Call the smoothing routine */

nqint = 10;
d06cac(nv1, nelt1, nedge1, coor1, edge1, conn1, nvfix, numfix,
        itrace, 0, nqint, &fail);

if (fail.code != NE_NOERROR)
{
    Vprintf("Error from d06cac.\\n%s\\n", fail.message);

```

```

        exit_status = 1;
        goto END;
    }

    /* Build the mesh of the 2nd domain */

    Vscanf("%ld", &nlines);
    Vscanf("%*[\n] ");

    /* Characteristic points of the boundary geometry */

    for (j = 1; j <= nlines; ++j) Vscanf("%lf", &COORCH(1,j));
    Vscanf("%*[\n] ");

    for (j = 1; j <= nlines; ++j) Vscanf("%lf", &COORCH(2,j));
    Vscanf("%*[\n] ");

    /* The lines of the boundary mesh */

    for (j = 1; j <= nlines; ++j)
    {
        for (i = 1; i <= 4; ++i) Vscanf("%ld", &LINED(i,j));
        Vscanf("%lf", &rate[j - 1]);
    }
    Vscanf("%*[\n] ");

    /* The number of connected components */
    /* to the boundary and their data */

    Vscanf("%ld", &ncomp);
    Vscanf("%*[\n] ");

    j = 1;
    for (i = 1; i <= ncomp; ++i)
    {
        Vscanf("%ld", &nlcomp[i - 1]);
        Vscanf("%*[\n] ");

        for (k = j; k <= j+abs(nlcomp[i-1])-1; ++k)
            Vscanf("%ld", &lcomp[k - 1]);
        Vscanf("%*[\n] ");
        j += abs(nlcomp[i-1]);
    }

    Vscanf(" ' %ls '", pmesh);
    Vscanf("%*[\n] ");

    itrace = 0;

    /* Call to the 2D boundary mesh generator */

    d06bac(nlines, coorch, lined, fbnd, coorus, nus, rate, ncomp,
          nlcomp, lcomp, nvmax, nedmx, &nvb2, coor2, &nedge2, edge2,
          itrace, 0, &comm, &fail);

    if (fail.code != NE_NOERROR)
    {
        Vprintf("Error from d06bac.\n%s\n", fail.message);
        exit_status = 1;
        goto END;
    }

    /* Generate mesh using the advancing front method */

    itrace = 0;

    d06acc(nvb2, nvint, nvmax, nedge2, edge2, &nv2, &nelt2, coor2,
          conn2, weight, itrace, 0, &fail);

    if (fail.code != NE_NOERROR)
    {

```

```

    Vprintf("Error from d06acc.\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}

for (k = 1; k <= nelt2; ++k) reft2[k - 1] = 2;

/* Rotation of the 2nd domain mesh */
/* to produce the 3rd mesh domain */

itype[0] = 3;
TRANS(1, 1) = 6.0;
TRANS(2, 1) = -1.0;
TRANS(3, 1) = -90.0;
itrace = 0;
mode = 0;

d06dac(mode, nv2, nedge2, nelt2, ntrans, itype, trans, coor2,
        edge2, conn2, coor3, edge3, conn3, itrace, 0, &fail);

if (fail.code != NE_NOERROR)
{
    Vprintf("Error from d06dac.\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}

nv3 = nv2;
nelt3 = nelt2;
nedge3 = nedge2;

for (k = 1; k <= nelt3; ++k) reft3[k - 1] = 3;

/* Restitching meshes 1 and 2 to form mesh 4 */

eps = 0.001;
itrace = 0;

d06dbc(eps, nv1, nelt1, nedge1, coor1, edge1, conn1, reft1, nv2,
        nelt2, nedge2, coor2, edge2, conn2, reft2, &nv4, &nelt4,
        &nedge4, coor4, edge4, conn4, reft4, itrace, 0, &fail);

if (fail.code != NE_NOERROR)
{
    Vprintf("Error from d06dbc.\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}

/* Restitching meshes 3 and 4 to form mesh 5 */

itrace = 0;

d06dbc(eps, nv4, nelt4, nedge4, coor4, edge4, conn4, reft4, nv3,
        nelt3, nedge3, coor3, edge3, conn3, reft3, &nv5, &nelt5,
        &nedge5, coor5, edge5, conn5, reft5, itrace, 0, &fail);

if (fail.code != NE_NOERROR)
{
    Vprintf("Error from d06dbc.\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}

if (pmesh[0] == 'N')
{
    Vprintf("The restitched mesh characteristics\n");
    Vprintf(" nv      =%6ld\n", nv5);
    Vprintf(" nelt   =%6ld\n", nelt5);
    Vprintf(" nedge  =%6ld\n", nedge5);
}

```

```

else if (pmesh[0] == 'Y')
{
    /* Output the mesh to view it using the NAG Graphics Library */
    Vprintf(" %10ld%10ld%10ld\n", nv5, nelt5, nedge5);

    for (i = 1; i <= nv5; ++i)
        Vprintf(" %12.6e %12.6e\n",
            COOR5(1,i), COOR5(2,i));

    for (k = 1; k <= nelt5; ++k)
        Vprintf("%10ld%10ld%10ld%10ld\n",
            CONN5(1,k), CONN5(2,k), CONN5(3,k), reft5[k - 1]);

    for (k = 1; k <= nedge5; ++k)
        Vprintf(" %10ld%10ld%10ld\n",
            EDGE5(1,k), EDGE5(2,k), EDGE5(3,k));
}
else
{
    Vprintf("Problem with the printing option Y or N\n");
}

END:

if (coor1) NAG_FREE(coor1);
if (coor2) NAG_FREE(coor2);
if (coor3) NAG_FREE(coor3);
if (coor4) NAG_FREE(coor4);
if (coor5) NAG_FREE(coor5);
if (coorch) NAG_FREE(coorch);
if (coorus) NAG_FREE(coorus);
if (rate) NAG_FREE(rate);
if (trans) NAG_FREE(trans);
if (weight) NAG_FREE(weight);
if (conn1) NAG_FREE(conn1);
if (conn2) NAG_FREE(conn2);
if (conn3) NAG_FREE(conn3);
if (conn4) NAG_FREE(conn4);
if (conn5) NAG_FREE(conn5);
if (edge1) NAG_FREE(edge1);
if (edge2) NAG_FREE(edge2);
if (edge3) NAG_FREE(edge3);
if (edge4) NAG_FREE(edge4);
if (edge5) NAG_FREE(edge5);
if (itype) NAG_FREE(itype);
if (lcomp) NAG_FREE(lcomp);
if (lined) NAG_FREE(lined);
if (nlcomp) NAG_FREE(nlcomp);
if (numfix) NAG_FREE(numfix);
if (reft1) NAG_FREE(reft1);
if (reft2) NAG_FREE(reft2);
if (reft3) NAG_FREE(reft3);
if (reft4) NAG_FREE(reft4);
if (reft5) NAG_FREE(reft5);

return exit_status;
}

static double fbnd(Integer i, double x, double y, Nag_Comm *pcomm)
{
    double radius2, x0, y0, ret_val;

    ret_val = 0.0;
    switch (i)
    {
        case 1:
            /* inner circle */

```

```

    x0 = 0.0;
    y0 = 0.0;
    radius2 = 1.0;
    ret_val = (x-x0)*(x-x0) + (y-y0)*(y-y0) - radius2;
    break;

case 2:

    /* outer circle */

    x0 = 0.0;
    y0 = 0.0;
    radius2 = 5.0;
    ret_val = (x-x0)*(x-x0) + (y-y0)*(y-y0) - radius2;
    break;
}

return ret_val;
}

```

Example 1 (ex1)

This example involves the unit square $[0, 1]^2$ meshed uniformly, and then translated by a vector $\vec{u} = \begin{pmatrix} u_1 \\ u_2 \end{pmatrix}$ (using `nag_mesh2d_trans (d06dac)`). This translated mesh is then restitched with the original mesh. Two cases are considered:

- (a) overlapping meshes ($u_1 = 15.0, u_2 = 17.0$),
- (b) partitioned meshes ($u_1 = 19.0, u_2 = 0.0$).

The mesh on the unit square has 400 vertices, 722 triangles and its boundary has 76 edges. In the overlapping case the resulting geometry is shown in Figure 1 and Figure 2. The resulting geometry for the partitioned meshes is shown in Figure 3.

Example 2 (ex2)

This example restitches three geometries by calling the function `nag_mesh2d_join (d06dbc)` twice. The result is a mesh with three partitions. The first geometry is meshed by the Delaunay-Voronoi process (using `nag_mesh2d_delaunay (d06abc)`), the second one meshed by an Advancing Front algorithm (using `nag_mesh2d_front (d06acc)`), while the third one is the result of a rotation (by $-\pi/2$) of the second one (using `nag_mesh2d_trans (d06dac)`). The resulting geometry is shown in Figure 4 and Figure 5.

9.1 Program Text

```

/* nag_mesh2d_join (d06dbc) Example Program.
 *
 * Copyright 2001 Numerical Algorithms Group.
 *
 * Mark 7, 2001.
 */

#include <stdio.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagd06.h>

static double fbnd(Integer , double , double , Nag_Comm *);

extern int ex1(void), ex2(void);

#define EDGE1(I,J) edge1[3*((J)-1)+(I)-1]
#define EDGE2(I,J) edge2[3*((J)-1)+(I)-1]
#define EDGE3(I,J) edge3[3*((J)-1)+(I)-1]
#define EDGE4(I,J) edge4[3*((J)-1)+(I)-1]
#define EDGE5(I,J) edge5[3*((J)-1)+(I)-1]
#define CONN1(I,J) conn1[3*((J)-1)+(I)-1]
#define CONN2(I,J) conn2[3*((J)-1)+(I)-1]
#define CONN3(I,J) conn3[3*((J)-1)+(I)-1]

```



```

#define CONN4(I,J) conn4[3*((J)-1)+(I)-1]
#define CONN5(I,J) conn5[3*((J)-1)+(I)-1]
#define COOR1(I,J) coor1[2*((J)-1)+(I)-1]
#define COOR2(I,J) coor2[2*((J)-1)+(I)-1]
#define COOR3(I,J) coor3[2*((J)-1)+(I)-1]
#define COOR4(I,J) coor4[2*((J)-1)+(I)-1]
#define COOR5(I,J) coor5[2*((J)-1)+(I)-1]
#define TRANS(I,J) trans[6*((J)-1)+(I)-1]
#define LINED(I,J) lined[4*((J)-1)+(I)-1]
#define COORCH(I,J) coorch[2*(J-1)+I-1]
#define COORUS(I,J) coorus[2*(J-1)+I-1]

int main(void)
{
    Vprintf("d06dbc Example Program Results\n");

    ex1();
    ex2();

    return 0;
}

int ex1(void)
{
    const Integer nvmax=900, nedmx=200, neltmx=2*nvmax+5, ntrans=1, mode=0;
    double eps;
    Integer exit_status, i, imax, itrace, itrans, jmax, jtrans, k, ktrans,
        nedgel, nedge2, nedge3, nelt1, nelt2, nelt3, nv1, nv2, nv3, reftk;
    Integer imaxml, jmaxml, ind;
    char pmesh[2];
    double *coor1=0, *coor2=0, *coor3=0, *trans=0;
    Integer *conn1=0, *conn2=0, *conn3=0, *edgel=0,
        *edge2=0, *edge3=0, *itype=0, *reft1=0, *reft2=0, *reft3=0;
    NagError fail;

    INIT_FAIL(fail);
    exit_status = 0;

    Vprintf("\nExample 1\n\n");

    /* Skip heading in data file */

    Vscanf("%*[\n] ");
    Vscanf("%*[\n] ");

    /* Read the mesh: coordinates and connectivity of the 1st domain */

    Vscanf("%ld", &nv1);
    Vscanf("%ld", &nelt1);
    Vscanf("%*[\n] ");

    nv2 = nv1;
    nelt2 = nelt1;

    imax = 20;
    jmax = imax;
    imaxml = imax - 1;
    jmaxml = jmax - 1;
    nedgel = 2*(imaxml + jmaxml);
    nedge2 = nedgel;

    /* Allocate memory */

    if ( !(coor1 = NAG_ALLOC(2*nv1, double)) ||
        !(coor2 = NAG_ALLOC(2*nv2, double)) ||
        !(coor3 = NAG_ALLOC(2*nvmax, double)) ||
        !(trans = NAG_ALLOC(6*ntrans, double)) ||
        !(conn1 = NAG_ALLOC(3*nelt1, Integer)) ||
        !(conn2 = NAG_ALLOC(3*nelt2, Integer)) ||
        !(conn3 = NAG_ALLOC(3*neltmx, Integer)) ||
        !(edgel = NAG_ALLOC(3*nedgel, Integer)) ||

```

```

        !(edge2 = NAG_ALLOC(3*nedge2, Integer)) ||
        !(edge3 = NAG_ALLOC(3*nedmx, Integer)) ||
        !(itype = NAG_ALLOC(ntrans, Integer)) ||
        !(reft1 = NAG_ALLOC(nelt1, Integer)) ||
        !(reft2 = NAG_ALLOC(nelt2, Integer)) ||
        !(reft3 = NAG_ALLOC(neltmx, Integer)) )
    {
        Vprintf("Allocation failure\n");
        exit_status = -1;
        goto END;
    }

    for (i = 1; i <= nv1; ++i)
    {
        Vscanf("%lf", &COOR1(1,i));
        Vscanf("%lf", &COOR1(2,i));
        Vscanf("%*[\n] ");
    }

    for (k = 1; k <= nelt1; ++k)
    {
        Vscanf("%ld", &CONN1(1,k));
        Vscanf("%ld", &CONN1(2,k));
        Vscanf("%ld", &CONN1(3,k));
        Vscanf("%ld", &reftk);
        Vscanf("%*[\n] ");

        reft1[k-1] = 1;
        reft2[k-1] = 2;
    }

    Vscanf(" ' %ls '", pmesh);
    Vscanf("%*[\n] ");

    /* the edges of the boundary */

    ind = 0;

    for (i = 1; i <= imaxm1; ++i)
    {
        ++ind;
        EDGE1(1,ind) = i;
        EDGE1(2,ind) = i + 1;
        EDGE1(3,ind) = 1;
    }

    for (i = 1; i <= jmaxm1; ++i)
    {
        ++ind;
        EDGE1(1,ind) = i*imax;
        EDGE1(2,ind) = (i+1)*imax;
        EDGE1(3,ind) = 1;
    }

    for (i = 1; i <= imaxm1; ++i)
    {
        ++ind;
        EDGE1(1,ind) = imax*jmax - i + 1;
        EDGE1(2,ind) = imax*jmax - i;
        EDGE1(3,ind) = 1;
    }

    for (i = 1; i <= jmaxm1; ++i)
    {
        ++ind;
        EDGE1(1,ind) = (jmax - i)*imax + 1;
        EDGE1(2,ind) = (jmax - i - 1)*imax + 1;
        EDGE1(3,ind) = 1;
    }

    for (ktrans = 0; ktrans < 2; ++ktrans)

```

```

{
/* Translation of the 1st domain to obtain the 2nd domain */
/* KTRANS = 0 leading to a domain overlapping */
/* KTRANS = 1 leading to a domain partition */

if (ktrans == 0)
{
    itrans = imax - 5;
    jtrans = jmax - 3;
}
else
{
    itrans = imax - 1;
    jtrans = 0;
}

itype[0] = 1;
TRANS(1, 1) = (double)itrans/(imax - 1.0);
TRANS(2, 1) = (double)jtrans/(jmax - 1.0);
itrace = 0;

d06dac(mode, nv2, nedge2, nelt2, ntrans, itype, trans, coor1,
        edge1, conn1, coor2, edge2, conn2, itrace, 0, &fail);

if (fail.code == NE_NOERROR)
{
    for (i = 1; i <= nedge2; ++i) EDGE2(3, i) = 2;

    /* Call to the restitching driver */

    itrace = 0;
    eps = 0.01;

    d06dbc(eps, nv1, nelt1, nedge1, coor1, edge1, conn1, reft1,
            nv2, nelt2, nedge2, coor2, edge2, conn2, reft2, &nv3,
            &nelt3, &nedge3, coor3, edge3, conn3, reft3, itrace,
            0, &fail);

    if (fail.code == NE_NOERROR)
    {
        if (pmesh[0] == 'N')
        {
            if (ktrans == 0)
            {
                Vprintf("The restitched mesh characteristics\n");
                Vprintf("in the overlapping case\n");
            }
            else
            {
                Vprintf("in the partition case\n");
            }
            Vprintf(" nv      =%6ld\n", nv3);
            Vprintf(" nelt   =%6ld\n", nelt3);
            Vprintf(" nedge  =%6ld\n", nedge3);
        }
        else if (pmesh[0] == 'Y')
        {

            /* Output the mesh to view it using the
               NAG Graphics Library */

            Vprintf(" %10ld%10ld%10ld\n", nv3, nelt3, nedge3);

            for (i = 1; i <= nv3; ++i)
                Vprintf(" %12.6e %12.6e\n",
                        COOR3(1,i), COOR3(2,i));

            for (k = 1; k <= nelt3; ++k)
                Vprintf(" %10ld%10ld%10ld%10ld\n",
                        CONN3(1,k), CONN3(2,k), CONN3(3,k), reft3[k - 1]);
        }
    }
}

```

```

        for (k = 1; k <= nedge3; ++k)
            Vprintf(" %10ld%10ld%10ld\n",
                    EDGE3(1,k), EDGE3(2,k), EDGE3(3,k));
    }
    else
    {
        Vprintf("Problem with the printing option Y or N\n");
        exit_status = -1;
        goto END;
    }
}
else
{
    Vprintf("Error from d06dbc.\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}
}
else
{
    Vprintf("Error from d06dac.\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}
}

END:

if (coor1) NAG_FREE(coor1);
if (coor2) NAG_FREE(coor2);
if (coor3) NAG_FREE(coor3);
if (trans) NAG_FREE(trans);
if (conn1) NAG_FREE(conn1);
if (conn2) NAG_FREE(conn2);
if (conn3) NAG_FREE(conn3);
if (edge1) NAG_FREE(edge1);
if (edge2) NAG_FREE(edge2);
if (edge3) NAG_FREE(edge3);
if (itype) NAG_FREE(itype);
if (reft1) NAG_FREE(reft1);
if (reft2) NAG_FREE(reft2);
if (reft3) NAG_FREE(reft3);

return exit_status;
}

int ex2(void)
{
    const Integer nvmax=900, nedmx=200, neltmx=2*nvmax+5,
        ntrans=1, nus=0, nvint=0, nvfix=0;
    double eps;
    Integer exit_status, i, itrace, j, k, l, ncomp, nedgel,
        nedge2, nedge3, nedge4, nedge5, nelt1, nelt2, nelt3,
        nelt4, nelt5, nlines, npropa, nqint, nv1, nv2, nv3, nv4,
        nv5, nvb1, nvb2, mode;
    char pmesh[2];
    double *coor1=0, *coor2=0, *coor3=0, *coor4=0, *coor5=0,
        *coorch=0, *coorus=0, *rate=0, *trans=0, *weight=0;
    Integer *conn1=0, *conn2=0, *conn3=0, *conn4=0, *conn5=0,
        *edge1=0, *edge2=0, *edge3=0, *edge4=0, *edge5=0, *itype=0,
        *lcomp=0, *lined=0, *nlcomp=0, *numfix=0, *reft1=0, *reft2=0,
        *reft3=0, *reft4=0, *reft5=0;
    NagError fail;
    Nag_Comm comm;

    INIT_FAIL(fail);
    exit_status = 0;

    Vprintf("\nExample 2\n\n");

    /* Skip heading in data file */

```

```

Vscanf("%*[^\\n] ");

/* Build the mesh of the 1st domain */
/* Initialise boundary mesh inputs: */
/* the number of line and of the characteristic points of */
/* the boundary mesh */

Vscanf("%ld", &nlines);
Vscanf("%*[^\\n] ");

/* Allocate memory */

if ( !(coor1 = NAG_ALLOC(2*nvmax, double)) ||
      !(coor2 = NAG_ALLOC(2*nvmax, double)) ||
      !(coor3 = NAG_ALLOC(2*nvmax, double)) ||
      !(coor4 = NAG_ALLOC(2*nvmax, double)) ||
      !(coor5 = NAG_ALLOC(2*nvmax, double)) ||
      !(coorch = NAG_ALLOC(2*nlines, double)) ||
      !(coorus = NAG_ALLOC(1, double)) ||
      !(rate = NAG_ALLOC(nlines, double)) ||
      !(trans = NAG_ALLOC(6*ntrans, double)) ||
      !(weight = NAG_ALLOC(1, double)) ||
      !(conn1 = NAG_ALLOC(3*neltmx, Integer)) ||
      !(conn2 = NAG_ALLOC(3*neltmx, Integer)) ||
      !(conn3 = NAG_ALLOC(3*neltmx, Integer)) ||
      !(conn4 = NAG_ALLOC(3*neltmx, Integer)) ||
      !(conn5 = NAG_ALLOC(3*neltmx, Integer)) ||
      !(edge1 = NAG_ALLOC(3*nedmx, Integer)) ||
      !(edge2 = NAG_ALLOC(3*nedmx, Integer)) ||
      !(edge3 = NAG_ALLOC(3*nedmx, Integer)) ||
      !(edge4 = NAG_ALLOC(3*nedmx, Integer)) ||
      !(edge5 = NAG_ALLOC(3*nedmx, Integer)) ||
      !(itype = NAG_ALLOC(ntrans, Integer)) ||
      !(lcomp = NAG_ALLOC(nlines, Integer)) ||
      !(lined = NAG_ALLOC(4*nlines, Integer)) ||
      !(numfix = NAG_ALLOC(1, Integer)) ||
      !(ref1 = NAG_ALLOC(2*nvmax+5, Integer)) ||
      !(ref2 = NAG_ALLOC(2*nvmax+5, Integer)) ||
      !(ref3 = NAG_ALLOC(2*nvmax+5, Integer)) ||
      !(ref4 = NAG_ALLOC(2*nvmax+5, Integer)) ||
      !(ref5 = NAG_ALLOC(2*nvmax+5, Integer)) )
{
    Vprintf("Allocation failure\\n");
    exit_status = -1;
    goto END;
}

/* Characteristic points of the boundary geometry */

for (j = 1; j <= nlines; ++j)
{
    Vscanf("%lf", &COORCH(1,j));
}
Vscanf("%*[^\\n] ");

for (j = 1; j <= nlines; ++j)
{
    Vscanf("%lf", &COORCH(2,j));
}
Vscanf("%*[^\\n] ");

/* The lines of the boundary mesh */

for (j = 1; j <= nlines; ++j)
{
    for (i = 1; i <= 4; ++i) Vscanf("%ld", &LINED(i,j));
    Vscanf("%lf", &rate[j - 1]);
}
Vscanf("%*[^\\n] ");

```

```

/* The number of connected components */
/* on the boundary and their data */

Vscanf("%ld", &ncomp);
Vscanf("%*[\n] ");

/* Allocate memory */

if ( !(nlcomp = NAG_ALLOC(ncomp, Integer)) )
{
    Vprintf("Allocation failure\n");
    exit_status = -1;
    goto END;
}

j = 1;

for (i = 1; i <= ncomp; ++i)
{
    Vscanf("%ld", &nlcomp[i - 1]);
    Vscanf("%*[\n] ");
    l = j + abs(nlcomp[i - 1]) - 1;
    for (k = j; k <= l; ++k) Vscanf("%ld", &lcomp[k - 1]);
    Vscanf("%*[\n] ");
    j += abs(nlcomp[i - 1]);
}

itrace = 0;

/* Call to the 2D boundary mesh generator */

d06bac(nlines, coorch, lined, fbnd, coorus, nus, rate, ncomp,
        nlcomp, lcomp, nvmax, nedmx, &nvbl, coor1, &nedge1,
        edgel, itrace, 0, &comm, &fail);

if (fail.code != NE_NOERROR)
{
    Vprintf("Error from d06bac.\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}

/* Generate mesh using Delaunay-Voronoi method */

/* Initialise mesh control parameters */

itrace = 0;
npropa = 1;

d06abc(nvbl, nvint, nvmax, nedge1, edgel, &nv1, &nelt1, coor1,
        conn1, weight, npropa, itrace, 0, &fail);

if (fail.code != NE_NOERROR)
{
    Vprintf("Error from d06abc.\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}

for (k = 1; k <= nelt1; ++k) reft1[k - 1] = 1;

/* Call the smoothing routine */

nqint = 10;
d06cac(nv1, nelt1, nedge1, coor1, edgel, conn1, nvfix, numfix,
        itrace, 0, nqint, &fail);

if (fail.code != NE_NOERROR)
{
    Vprintf("Error from d06cac.\n%s\n", fail.message);
    exit_status = 1;
}

```

```

    goto END;
}

/* Build the mesh of the 2nd domain */

Vscanf("%ld", &nlines);
Vscanf("%*[\n] ");

/* Characteristic points of the boundary geometry */

for (j = 1; j <= nlines; ++j) Vscanf("%lf", &COORCH(1,j));
Vscanf("%*[\n] ");

for (j = 1; j <= nlines; ++j) Vscanf("%lf", &COORCH(2,j));
Vscanf("%*[\n] ");

/* The lines of the boundary mesh */

for (j = 1; j <= nlines; ++j)
{
    for (i = 1; i <= 4; ++i) Vscanf("%ld", &LINED(i,j));
    Vscanf("%lf", &rate[j - 1]);
}
Vscanf("%*[\n] ");

/* The number of connected components */
/* to the boundary and their data */

Vscanf("%ld", &ncomp);
Vscanf("%*[\n] ");

j = 1;
for (i = 1; i <= ncomp; ++i)
{
    Vscanf("%ld", &nlcomp[i - 1]);
    Vscanf("%*[\n] ");

    for (k = j; k <= j+abs(nlcomp[i-1])-1; ++k)
        Vscanf("%ld", &lcomp[k - 1]);
    Vscanf("%*[\n] ");
    j += abs(nlcomp[i-1]);
}

Vscanf(" ' %ls '", pmesh);
Vscanf("%*[\n] ");

itrace = 0;

/* Call to the 2D boundary mesh generator */

d06bac(nlines, coorch, lined, fbnd, coorus, nus, rate, ncomp,
        nlcomp, lcomp, nvmax, nedmx, &nvb2, coor2, &nedge2, edge2,
        itrace, 0, &comm, &fail);

if (fail.code != NE_NOERROR)
{
    Vprintf("Error from d06bac.\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}

/* Generate mesh using the advancing front method */

itrace = 0;

d06acc(nvb2, nvint, nvmax, nedge2, edge2, &nv2, &nelt2, coor2,
        conn2, weight, itrace, 0, &fail);

if (fail.code != NE_NOERROR)
{
    Vprintf("Error from d06acc.\n%s\n", fail.message);

```

```

        exit_status = 1;
        goto END;
    }

    for (k = 1; k <= nelt2; ++k) reft2[k - 1] = 2;

    /* Rotation of the 2nd domain mesh */
    /* to produce the 3rd mesh domain */

    itype[0] = 3;
    TRANS(1, 1) = 6.0;
    TRANS(2, 1) = -1.0;
    TRANS(3, 1) = -90.0;
    itrace = 0;
    mode = 0;

    d06dac(mode, nv2, nedge2, nelt2, ntrans, itype, trans, coor2,
           edge2, conn2, coor3, edge3, conn3, itrace, 0, &fail);

    if (fail.code != NE_NOERROR)
    {
        Vprintf("Error from d06dac.\n%s\n", fail.message);
        exit_status = 1;
        goto END;
    }

    nv3 = nv2;
    nelt3 = nelt2;
    nedge3 = nedge2;

    for (k = 1; k <= nelt3; ++k) reft3[k - 1] = 3;

    /* Restitching meshes 1 and 2 to form mesh 4 */

    eps = 0.001;
    itrace = 0;

    d06dbc(eps, nv1, nelt1, nedge1, coor1, edge1, conn1, reft1, nv2,
           nelt2, nedge2, coor2, edge2, conn2, reft2, &nv4, &nelt4,
           &nedge4, coor4, edge4, conn4, reft4, itrace, 0, &fail);

    if (fail.code != NE_NOERROR)
    {
        Vprintf("Error from d06dbc.\n%s\n", fail.message);
        exit_status = 1;
        goto END;
    }

    /* Restitching meshes 3 and 4 to form mesh 5 */

    itrace = 0;

    d06dbc(eps, nv4, nelt4, nedge4, coor4, edge4, conn4, reft4, nv3,
           nelt3, nedge3, coor3, edge3, conn3, reft3, &nv5, &nelt5,
           &nedge5, coor5, edge5, conn5, reft5, itrace, 0, &fail);

    if (fail.code != NE_NOERROR)
    {
        Vprintf("Error from d06dbc.\n%s\n", fail.message);
        exit_status = 1;
        goto END;
    }

    if (pmesh[0] == 'N')
    {
        Vprintf("The restitched mesh characteristics\n");
        Vprintf(" nv      =%6ld\n", nv5);
        Vprintf(" nelt   =%6ld\n", nelt5);
        Vprintf(" nedge =%6ld\n", nedge5);
    }
    else if (pmesh[0] == 'Y')

```



```

{
    /* Output the mesh to view it using the NAG Graphics Library */
    Vprintf(" %10ld%10ld%10ld\n", nv5, nelt5, nedge5);

    for (i = 1; i <= nv5; ++i)
        Vprintf(" %12.6e %12.6e\n",
            COOR5(1,i), COOR5(2,i));

    for (k = 1; k <= nelt5; ++k)
        Vprintf("%10ld%10ld%10ld%10ld\n",
            CONN5(1,k), CONN5(2,k), CONN5(3,k), reft5[k - 1]);

    for (k = 1; k <= nedge5; ++k)
        Vprintf(" %10ld%10ld%10ld\n",
            EDGE5(1,k), EDGE5(2,k), EDGE5(3,k));
}
else
{
    Vprintf("Problem with the printing option Y or N\n");
}
}

END:

if (coor1) NAG_FREE(coor1);
if (coor2) NAG_FREE(coor2);
if (coor3) NAG_FREE(coor3);
if (coor4) NAG_FREE(coor4);
if (coor5) NAG_FREE(coor5);
if (coorch) NAG_FREE(coorch);
if (coorus) NAG_FREE(coorus);
if (rate) NAG_FREE(rate);
if (trans) NAG_FREE(trans);
if (weight) NAG_FREE(weight);
if (conn1) NAG_FREE(conn1);
if (conn2) NAG_FREE(conn2);
if (conn3) NAG_FREE(conn3);
if (conn4) NAG_FREE(conn4);
if (conn5) NAG_FREE(conn5);
if (edge1) NAG_FREE(edge1);
if (edge2) NAG_FREE(edge2);
if (edge3) NAG_FREE(edge3);
if (edge4) NAG_FREE(edge4);
if (edge5) NAG_FREE(edge5);
if (itype) NAG_FREE(itype);
if (lcomp) NAG_FREE(lcomp);
if (lined) NAG_FREE(lined);
if (nlcomp) NAG_FREE(nlcomp);
if (numfix) NAG_FREE(numfix);
if (reft1) NAG_FREE(reft1);
if (reft2) NAG_FREE(reft2);
if (reft3) NAG_FREE(reft3);
if (reft4) NAG_FREE(reft4);
if (reft5) NAG_FREE(reft5);

return exit_status;
}

static double fbnd(Integer i, double x, double y, Nag_Comm *pcomm)
{
    double radius2, x0, y0, ret_val;

    ret_val = 0.0;
    switch (i)
    {
        case 1:
            /* inner circle */

            x0 = 0.0;

```

```

    y0 = 0.0;
    radius2 = 1.0;
    ret_val = (x-x0)*(x-x0) + (y-y0)*(y-y0) - radius2;
    break;

case 2:

    /* outer circle */

    x0 = 0.0;
    y0 = 0.0;
    radius2 = 5.0;
    ret_val = (x-x0)*(x-x0) + (y-y0)*(y-y0) - radius2;
    break;
}

return ret_val;
}

```

9.2 Program Data

Note: since the data file for this example is quite large only a section of it is reproduced in this document. The full data file is distributed with your implementation.

D06DBF Example Program Data

Example 1

```

    400      722      :NV1 NELT1
    0.000000E+00  0.000000E+00
      .
      .
      .
    0.100000E+01  0.100000E+01      :COOR1(1:2,1:NV1)
      1          2          22      0
      .
      .
      .
    379      400      399      0 : (CONN1(:,K), REFT, K = 1,...,NELT1)
'N'          : Printing option 'Y' or 'N'

```

9.3 Program Results

d06dbc Example Program Results

Example 1

The restitched mesh characteristics
in the overlapping case

```

nv   = 785
nelt = 1428
nedge = 152

```

in the partition case

```

nv   = 780
nelt = 1444
nedge = 133

```

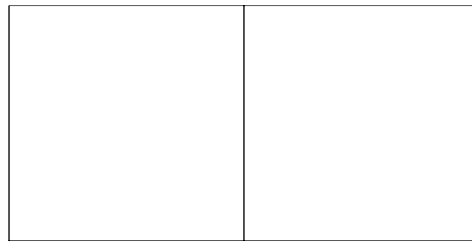
Example 2

The restitched mesh characteristics

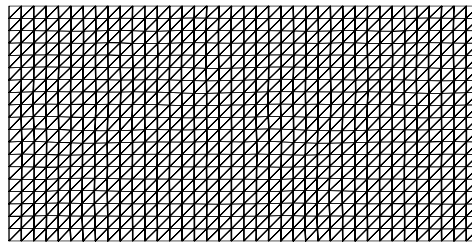
```

nv   = 643
nelt = 1133
nedge = 171

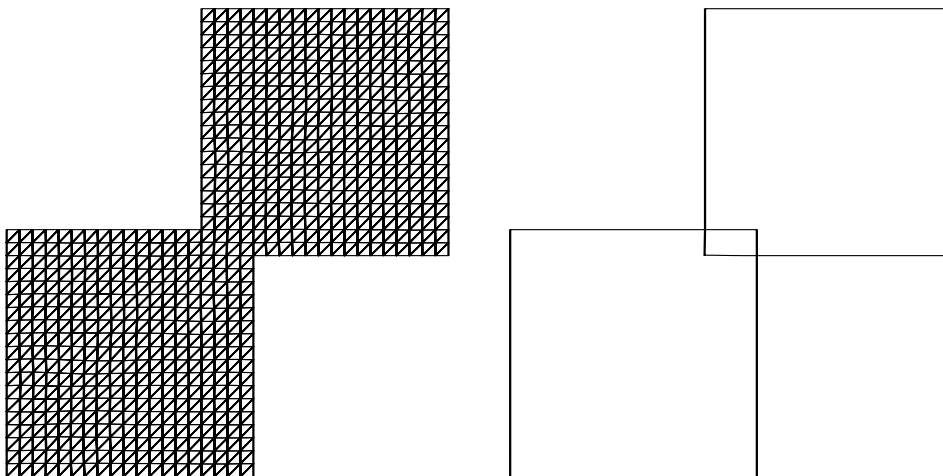
```

**Figure 1**

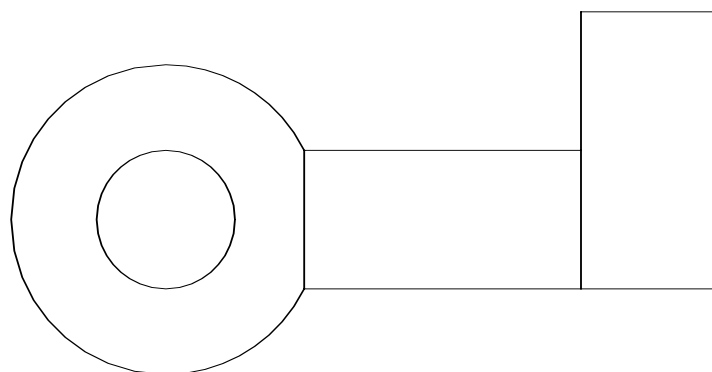
The boundary and the interior interfaces of the two partitioned squares geometry

**Figure 2**

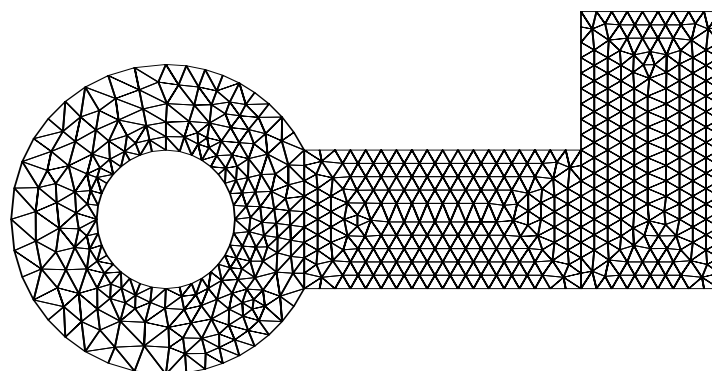
The interior mesh of the two partitioned squares geometry

**Figure 3**

The boundary and the interior interfaces (left); the interior mesh (right)
of the two overlapping squares geometry

**Figure 4**

The boundary and the interior interfaces of the double restitched geometry

**Figure 5**

The interior mesh of the double restitched geometry
