e01 - Interpolation

nag_2d_scat_eval (e01sbc)

1. Purpose

nag_2d_scat_eval (e01sbc) evaluates at given points the two-dimensional interpolant function computed by nag_2d_scat_interpolant (e01sac).

2. Specification

3. Description

This function takes as input the parameters defining the interpolant F(x,y) of a set of scattered data points (x_r, y_r, f_r) , for r = 1, 2, ..., m, as computed by nag_2d_scat_interpolant (e01sac), and evaluates the interpolant at each of the points (px_k, py_k) , for k = 1, 2, ..., n.

When **method** = **Nag_RC**, the derivatives stored in **comm** will be used to compute the interpolant if necessary. A triangle is sought which contains the point (px_k, py_k) , and the vertices of the triangle along with the partial derivatives and f_r values at the vertices are used to compute the value $F(px_k, py_k)$. If the point (px_k, py_k) lies outside the triangulation defined by the input parameters, the returned value is obtained by extrapolation. In this case, the interpolating function F is extended linearly beyond the triangulation boundary. The method is described in more detail in Renka and Cline (1984) and the code is derived from Renka (1984).

Alternatively, if $\mathbf{method} = \mathbf{Nag_Shep}$, then all points that are within distance of (px_k, py_k) , along with the corresponding nodal functions stored in \mathbf{comm} , will be used to compute a value of the interpolant, if necessary.

nag_2d_scat_eval must only be called after a call to nag_2d_scat_interpolant (e01sac).

4. Parameters

comm

Pointer to a communication structure of type Nag_Scat_Struct which must be unchanged from the previous call of nag_2d_scat_interpolant (e01sac).

n

Input: the number of points at which the evaluation of the interpolant is required. Constraint: $n \ge 1$.

px[n]

py[n]

Input: the x- and y-coordinates of the kth point (px_k, py_k) , for $k = 1, 2, ..., \mathbf{n}$, at which the interpolant is to be evaluated.

pf[n]

Output: the values of the interpolant evaluated at the points (px_k, py_k) , for $k = 1, 2, \dots, n$.

fail

The NAG error parameter, see the Essential Introduction to the NAG C Library.

5. Error Indications and Warnings

NE_NO_SETUP

The setup function nag_2d_scat_interpolant (e01sac) has not been called.

NE_SETUP_ERROR

The call to setup function nag_2d_scat_interpolant (e01sac) produced an error.

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NE_STRUCT_CORRUPT

The structure $\langle value \rangle$ has been corrupted since the previous call to $\langle value \rangle$.

NE_INT_ARG_LT

On entry, **n** must not be less than 1: $\mathbf{n} = \langle value \rangle$

NW_VALUE_EXTRAPOLATED

The evaluation point ($\langle value \rangle$, $\langle value \rangle$) of (px, py) lies outside the triangulation boundary. The returned value, $\langle value \rangle$, of **pf** was computed by extrapolation.

NE_BAD_INTERPOLANT

On entry, the interpolant cannot be evaluated because the evaluation point (px, py) of $(\langle value \rangle, \langle value \rangle)$ is outside the support region of the input data points defined by **optional.rnw**= $\langle value \rangle$ as set in nag_2d_scat_interpolant (e01sac).

6. Further Comments

The time taken for a call of nag_2d_scat_eval is approximately proportional to the number of data points, m, used by nag_2d_scat_interpolant (e01sac).

The results returned by this function are particularly suitable for applications such as graph plotting, producing a smooth surface from a number of scattered points.

6.1. Accuracy

Computational errors should be negligible in most practical situations.

6.2. References

Franke R and Nielson G (1980) Smooth Interpolation of Large Sets of Scattered Data Internat. J. Num. Methods Engrg. 15 1691–1704.

Renka R L (1984) Algorithm 624: Triangulation and Interpolation of Arbitrarily Distributed Points in the Plane ACM Trans. Math. Softw. 10 440–442.

Renka R L and Cline A K (1984) A Triangle-based C^1 Interpolation Method Rocky Mountain J. Math. 14 223–237.

Shepard D (1968) A Two-dimensional Interpolation Function for Irregularly Spaced Data *Proc.* 23rd Nat. Conf. ACM Brandon/Systems Press Inc, Princeton pp 517–523.

7. See Also

nag_2d_scat_interpolant (e01sac)

8. Example

See the example program for nag_2d_scat_interpolant (e01sac).

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