

nag_real_lu (f03afc)

1. Purpose

nag_real_lu (f03afc) computes an LU factorization of a real matrix, with partial pivoting, and evaluates the determinant.

2. Specification

```
#include <nag.h>
#include <nagf03.h>
```

```
void nag_real_lu(Integer n, double a[], Integer tda, Integer pivot[],
                 double *detf, Integer *dete, NagError *fail)
```

3. Description

This function computes an LU factorization of a real matrix A with partial pivoting: $PA = LU$, where P is a permutation matrix, L is lower triangular and U is unit upper triangular. The determinant of A is the product of the diagonal elements of L with the correct sign determined by the row interchanges.

4. Parameters

n

Input: n , the order of the matrix A .
Constraint: $n \geq 1$.

a[n][tda]

Input: the n by n matrix A .
Output: A is overwritten by the lower triangular matrix L and the off-diagonal elements of the upper triangular matrix U . The unit diagonal elements of U are not stored.

tda

Input: the second dimension of the array **a** as declared in the function from which **nag_real_lu** is called.
Constraint: **tda** \geq **n**.

pivot[n]

Output: **pivot**[$i - 1$] gives the row index of the i th pivot.

detf

dete

Output: the determinant of A is given by **detf** \times $2.0^{\mathbf{dete}}$. It is given in this form to avoid overflow or underflow.

fail

The NAG error parameter, see the Essential Introduction to the NAG C Library.

5. Error Indications and Warnings

NE_SINGULAR

The matrix A is singular, possibly due to rounding errors. The factorization could not be completed. **detf** and **dete** are set to zero.

NE_INT_ARG_LT

On entry, **n** must not be less than 1: **n** = *value*.

NE_2_INT_ARG_LT

On entry, **tda** = *value* while **n** = *value*. The parameters must satisfy **tda** \geq **n**.

NE_ALLOC_FAIL

Memory allocation failed.

6. Further Comments

The time taken by the function is approximately proportional to n^3 .

6.1. Accuracy

The accuracy of the determinant depends on the conditioning of the original matrix. For a detailed error analysis, see Wilkinson and Reinsch (1971) p 107.

6.2. References

Wilkinson J H and Reinsch C (1971) *Handbook for Automatic Computation (Vol II, Linear Algebra)* Springer-Verlag pp 93-110.

7. See Also

nag_real_lu_solve_mult_rhs (f04ajc)

8. Example

To compute the LU factorization with partial pivoting, and calculate the determinant, of the real matrix

$$\begin{pmatrix} 33 & 16 & 72 \\ -24 & -10 & -57 \\ -8 & -4 & -17 \end{pmatrix}.$$

8.1. Program Text

```

/* nag_real_lu(f03afc) Example Program
 *
 * Copyright 1990 Numerical Algorithms Group.
 *
 * Mark 2 revised, 1992.
 */

#include <nag.h>
#include <math.h>
#include <stdio.h>
#include <nag_stdlib.h>
#include <nagf03.h>

#define NMAX 8
#define TDA NMAX

main()
{
    double detf, two=2.0;
    Integer i, dete, j, n;
    static NagError fail;
    double a[NMAX][TDA];
    Integer pivot[NMAX];

    Vprintf("f03afc Example Program Results\n");
    /* Skip heading in data file */
    Vscanf("%*[\n]");
    Vscanf("%ld",&n);

    if (n>0 && n<=NMAX)
    {
        for (i=0; i<n; i++)
            for (j=0; j<n; j++)
                Vscanf("%lf",&a[i][j]);
        fail.print = TRUE;
        f03afc(n,(double *)a,(Integer)TDA,pivot,&detf,&dete,&fail);
        if (fail.code!=NE_NOERROR)
            exit(EXIT_FAILURE);
        else

```

```

    {
        Vprintf("Array A after factorization\n");
        for (i=0; i<n; i++)
            for (j=0; j<n; j++)
                Vprintf("%9.4f%s",a[i][j],(j%8==7 || j==n-1) ? "\n" : " ");
        Vprintf("\nArray P\n");
        for (i=0; i<n; i++)
            Vprintf("%3ld%s",pivot[i],(i%8==7 || i==n-1) ? "\n" : " ");
        Vprintf("\ndetf = %9.4f  dete = %2ld\n", detf, dete);
        detf = detf * pow(two, (double)dete);
        Vprintf("\nValue of determinant = %9.4f\n", detf);
    }
}
exit(EXIT_SUCCESS);
}

```

8.2. Program Data

f03afc Example Program Data

```

3
 33  16  72
-24 -10 -57
 -8  -4 -17

```

8.3. Program Results

f03afc Example Program Results

```

Array A after factorization
-8.0000  0.5000  2.1250
-24.0000  2.0000 -3.0000
 33.0000 -0.5000  0.3750

```

```

Array P
 3  2  3

```

```

detf = 0.3750  dete = 4

```

```

Value of determinant = 6.0000

```
