## 1. Purpose

 $nag_shapiro_wilk_test$  (g01ddc) calculates Shapiro and Wilk's W statistic and its significance level for testing Normality.

## 2. Specification

```
#include <nag.h>
#include <nagg01.h>
```

## 3. Description

This routine calculates Shapiro and Wilk's W statistic and its significance level for any sample size between 3 and 2000. It is an adaptation of the Applied Statistics Algorithm AS 181, see Royston (1982a). The full description of the theory behind this algorithm is given in Royston (1982b).

Given a set of observations  $x_1, x_2, \ldots, x_n$  sorted into either ascending or descending order (nag\_double\_sort (m01cac) may be used to sort the data), nag\_shapiro\_wilk\_test calculates the value of Shapiro and Wilk's W statistic defined as:

$$W = \frac{\left(\sum_{i=1}^{n} a_i x_i\right)^2}{\sum_{i=1}^{n} \left(x_i - \bar{x}\right)^2}$$

where  $\bar{x} = \frac{1}{n} \sum_{i=1}^{n} x_i$  is the sample mean and  $a_i$ , for i = 1, 2, ..., n are a set of 'weights' whose values depend only on the sample size n.

On exit, the values of  $a_i$ , for i = 1, 2, ..., n are only of interest should the user wish to call the routine again to calculate W and its significance level for a different sample of the same size.

#### 4. Parameters

#### $\mathbf{n}$

Input: the sample size, n. Constraint:  $3 \le \mathbf{n} \le 2000$ .

## $\mathbf{x}[\mathbf{n}]$

Input: the ordered sample values,  $x_i$ ; for i = 1, 2, ..., n.

#### calc\_wts

Input: calc\_wts must be set to TRUE if the user wishes nag\_shapiro\_wilk\_test to calculate the elements of **a**.

**calc\_wts** should be set to **FALSE** if the user has saved the values in **a** from a previous call to nag\_shapiro\_wilk\_test.

If in doubt, set **calc\_wts** equal to **TRUE**.

a[n]

Input: if **calc\_wts** has been set to **FALSE** then before entry **a** must contain the n weights as calculated in a previous call to nag\_shapiro\_wilk\_test, otherwise **a** need not be set. Output: the n weights required to calculate W.

w

```
Output: the value of the statistic, W.
```

3.g01ddc.1

pw

Output: the significance level of W.

### fail

The NAG error parameter, see the Essential Introduction to the NAG C Library.

# 5. Error Indications and Warnings

## NE\_INT\_ARG\_LT

On entry, **n** must not be less than 3:  $\mathbf{n} = \langle value \rangle$ .

### NE\_INT\_ARG\_GT

On entry, **n** must not be greater than 2000:  $\mathbf{n} = \langle value \rangle$ .

## NE\_NON\_MONOTONIC

On entry, the sequence in array **x** is non-monotonic. First anomaly detected at  $\mathbf{x}[\langle value \rangle] = \langle value \rangle$ .

### NE\_ALL\_ELEMENTS\_EQUAL

On entry, all the values in the array  $\mathbf{x}$  must not be equal.

## NE\_INTERNAL\_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please consult NAG for assistance.

### 6. Further Comments

The time taken by the routine depends roughly linearly on the value of n.

For very small samples the power of the test may not be very high.

The contents of the array A should not be modified between calls to nag\_shapiro\_wilk\_test for a given sample size, unless **calc\_wts** is reset to **TRUE** before each call of nag\_shapiro\_wilk\_test.

The Shapiro and Wilk W test is very sensitive to ties. If the data has been rounded the test can be improved by using Sheppard's correction to adjust the sum of squares about the mean. This produces an adjusted value of W,

$$WA = W \frac{\sum (x_{(i)} - \bar{x})^2}{\left\{ \sum_{i=1}^n (x_{(i)} - \bar{x})^2 - \frac{n-1}{12} \omega^2 \right\}}$$

where  $\omega$  is the rounding width. WA can be compared with a standard normal distribution, but a further approximation is given by Royston (1986).

## 6.1. Accuracy

There may be a loss of significant figures for large n.

#### 6.2. References

Royston J P (1982a) Algorithm AS181: The W Test for Normality Appl. Statist. **31** 176–180. Royston J P (1982b) An extension of Shapiro and Wilk's W Test for Normality to large samples Appl. Statist. **31** 115–124.

Royston J P (1986) A Remark on AS181: The W Test for Normality Appl. Statist. 35 232–234.

## 7. See Also

nag\_ranks\_and\_scores (g01dhc)

## 8. Example

A program to test the following 2 samples (each of size 20) for Normality.

Sample	Data
Number	
(1)	$\begin{array}{l} 0.11, 7.87, 4.61, 10.14, 7.95, 3.14, 0.46, 4.43, 0.21, 4.75, 0.71, 1.52, 3.24, 0.93,\\ 0.42, 4.97, 9.53, 4.55, 0.47, 6.66 \end{array}$
(2)	1.36, 1.14, 2.92, 2.55, 1.46, 1.06, 5.27, -1.11, 3.48, 1.10, 0.88, -0.51, 1.46, 0.52, 6.20, 1.69, 0.08, 3.67, 2.81, 3.49

The elements of  $\mathbf{a}$  are calculated only in the first call of nag\_shapiro\_wilk\_test and are re-used in the second call.

#### 8.1. Program Text

```
/* nag_shapiro_wilk_test(g01ddc) Example Program.
 * Copyright 1996 Numerical Algorithms Group.
 *
 * Mark 4, 1996.
 *
 */
#include <nag.h>
#include <nag_stdlib.h>
#include <stdio.h>
#include <nagg01.h>
#include <nagm01.h>
main()
{
#define NMAX 20
  /* Local variables */
  double a[NMAX];
  Integer i, j, n;
double w, x[NMAX], pw;
  Boolean calwts;
  Vprintf("g01ddc Example Program Results\n");
  /*
          Skip heading in data file */
  Vscanf("%*[^\n] ");
  calwts = TRUE;
  Vscanf("%ld ", &n);
if (n > 0 && n <= NMAX)
     {
       for (j = 1; j <= 2; ++j)
         {
           for (i = 1; i <= n; ++i)
             Vscanf("%lf ", &x[i - 1]);
           m01cac(x, (size_t)n, Nag_Ascending,NAGERR_DEFAULT);
g01ddc(n, x, calwts, a, &w, &pw, NAGERR_DEFAULT);
           Vprintf("\n For sample number %21d, value of W statistic = %7.4f\n",
           j,w);
Vprintf("
                                                Significance level is %8.4f\n", pw);
           calwts = FALSE;
         3
    }
  exit(EXIT_SUCCESS);
}
```

# 8.2. Program Data

g01ddc Example Program Data 20

 $0.11 \ \ 7.87 \ \ 4.61 \ \ 10.14 \ \ \ 7.95 \ \ 3.14 \ \ 0.46 \ \ 4.43 \ \ 0.21 \ \ 4.75 \\ 0.71 \ \ 1.52 \ \ 3.24 \ \ 0.93 \ \ 0.42 \ \ 4.97 \ \ 9.53 \ \ 4.55 \ \ 0.47 \ \ 6.66 \\ 1.36 \ \ 1.14 \ \ 2.92 \ \ 2.55 \ \ 1.46 \ \ 1.06 \ \ 5.27 \ \ -1.11 \ \ 3.48 \ \ 1.10 \\ 0.88 \ \ -0.51 \ \ 1.46 \ \ 0.52 \ \ 6.20 \ \ 1.69 \ \ 0.08 \ \ 3.67 \ \ 2.81 \ \ 3.49$ 

### 8.3. Program Results

g01ddc Example Program Results

For sample number 1, value of W statistic = 0.8992 Significance level is 0.0408 For sample number 2, value of W statistic = 0.9583 Significance level is 0.5171