

# NAG C Library Function Document

## nag\_mills\_ratio (g01mbc)

### 1 Purpose

nag\_mills\_ratio (g01mbc) returns the reciprocal of Mills' Ratio.

### 2 Specification

```
double nag_mills_ratio (double x)
```

### 3 Description

nag\_mills\_ratio (g01mbc) calculates the reciprocal of Mills' Ratio, the hazard rate,  $\lambda(x)$ , for the standard Normal distribution. It is defined as the ratio of the ordinate to the upper tail area of the standard Normal distribution, that is,

$$\lambda(x) = \frac{Z(x)}{Q(x)} = \frac{\frac{1}{\sqrt{2\pi}} e^{-(x^2/2)}}{\frac{1}{\sqrt{2\pi}} \int_x^\infty e^{-(t^2/2)} dt}.$$

If  $x \leq 9.0$ , then the calculation is based on a Chebyshev expansion as described in nag\_erfc (s15adc); otherwise, the method due to Swan (1969) is used.

### 4 References

Gross A J and Clark V A (1975) *Survival Distributions: Reliability Applications in the Biomedical Sciences* Wiley

Swan A V (1969) Algorithm AS17. The reciprocal of Mills's ratio *Appl. Statist.* **18** 115

### 5 Parameters

1:	$x$ – double	<i>Input</i>
----	--------------	--------------

*On entry:* the argument of the reciprocal of Mills' Ratio,  $x$ .

### 6 Error Indicators and Warnings

None.

### 7 Accuracy

In the left-hand tail,  $x < 0.0$ , if  $\frac{1}{2} e^{-(1/2)x^2} \leq$  the safe range parameter (nag\_real\_safe\_small\_number (X02AMC)), then 0.0 is returned, which is close to the true value.

The relative accuracy is bounded by the effective **machine precision**. See nag\_erfc (s15adc) for further discussion for the case  $x \leq 9.0$ .

### 8 Further Comments

If, before entry,  $x$  is not a standard Normal variable, it has to be standardized, and on exit, nag\_mills\_ratio (g01mbc) has to be divided by the standard deviation. That is, if the Normal distribution has mean  $\mu$  and variance  $\sigma^2$ , then its hazard rate,  $\lambda(x; \mu, \sigma^2)$ , is given by

$$\lambda(x; \mu, \sigma^2) = \lambda((x - \mu)/\sigma)/\sigma.$$

## 9 Example

The hazard rate is evaluated at different values of  $x$  for Normal distributions with different means and variances. The results are then printed.

### 9.1 Program Text

```
/* nag_mills_ratio (g01mbc) Example Program.
 *
 * Copyright 2001 Numerical Algorithms Group.
 *
 * Mark 7, 2001.
 */

#include <stdio.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagg01.h>

int main(void)
{
    /* Scalars */
    double rm, x, xmu, xsig, z__;
    Integer exit_status, i;

    exit_status = 0;
    Vprintf("g01mbc Example Program Results\n");

    /* Skip heading in data file */
    Vscanf("%*[^\n] ");

    Vprintf("\n%2sMean%5sSigma%4sX%8sReciprocal", "", "", "", "");
    Vprintf("\n                                  Mills Ratio\n\n");
    for (i = 1; i <= 3; ++i)
    {
        Vscanf("%lf%lf%lf*[^\n] ", &x, &xmu, &xsig);
        z__ = (x - xmu) / xsig;
        rm = g01mbc(z__) / xsig;
        Vprintf("%7.4f%2s%7.4f%2s%7.4f%2s%7.4f", xmu, "", xsig, "", x, "", rm);
        Vprintf("\n");
    }
    return exit_status;
}
```

### 9.2 Program Data

```
g01mbc Example Program Data
0.0 0.0 1.0
-2.0 1.0 2.5
10.3 9.0 1.6
```

### 9.3 Program Results

```
g01mbc Example Program Results
```

Mean	Sigma	X	Reciprocal Mills Ratio
0.0000	1.0000	0.0000	0.7979
1.0000	2.5000	-2.0000	0.0878
9.0000	1.6000	10.3000	0.8607

---