

nag_glm_tran_model (g02gkc)

1. Purpose

nag_glm_tran_model (g02gkc) calculates the estimates of the parameters of a generalized linear model for given constraints from the singular value decomposition results.

2. Specification

```
#include <nag.h>
#include <nagg02.h>

void nag_glm_tran_model(Integer ip, Integer nclin, double v[],
                        Integer tdv, double c[], Integer tdc, double b[], double scale,
                        double se[], double cov[], NagError *fail)
```

3. Description

This function computes the estimates given a set of linear constraints for a generalized linear model which is not of full rank. It is intended for use after a call to `nag_glm_normal (g02gac)`, `nag_glm_binomial (g02gbc)`, `nag_glm_poisson (g02gcc)` or `nag_glm_gamma (g02gdc)`.

In the case of a model not of full rank the functions use a singular value decomposition (SVD) to find the parameter estimates, $\hat{\beta}_{svd}$, and their variance-covariance matrix. Details of the SVD are made available, in the form of the matrix P^* :

$$P^* = \begin{pmatrix} D^{-1}P_1^T \\ P_0^T \end{pmatrix}$$

as described by `nag_glm_normal (g02gac)`, `nag_glm_binomial (g02gbc)`, `nag_glm_poisson (g02gcc)` and `nag_glm_gamma (g02gdc)`.

Alternative solutions can be formed by imposing constraints on the parameters. If there are p parameters and the rank of the model is k , then $n_c = p - k$ constraints will have to be imposed to obtain a unique solution.

Let C be a p by n_c matrix of constraints, such that

$$C^T \beta = 0,$$

then the new parameter estimates $\hat{\beta}_c$ are given by:

$$\begin{aligned} \hat{\beta}_c &= A\hat{\beta}_{svd} \\ &= (I - P_0(C^T P_0)^{-1})\hat{\beta}_{svd}, \end{aligned}$$

where I is the identity matrix, and the variance-covariance matrix is given by:

$$AP_1 D^{-2} P_1^T A^T$$

provided $(C^T P_0)^{-1}$ exists.

4. Parameters

ip

Input: the number of terms in the linear model, p .

Constraint: **ip** ≥ 1 .

nclin

Input: the number of constraints to be imposed on the parameters, n_c .

Constraint: **0** < **nclin** < **ip**.

v[ip][tdv]

Input: **v** as returned by `nag_glm_normal (g02gac)`, `nag_glm_binomial (g02gbc)`, `nag_glm_poisson (g02gcc)` or `nag_glm_gamma (g02gdc)`.

tdv

Input: the second dimension of the array **v** as declared in the function from which nag_glm_tran_model is called.

Constraint: **tdv** $\geq$ **ip**+6. **tdv** should be as supplied to nag_glm_normal (g02gac), nag_glm_binomial (g02gbc), nag_glm_poisson (g02gcc) or nag_glm_gamma (g02gdc).

c[ip][tdc]

Input: the **nclin** constraints stored by column, i.e., the *i*th constraint is stored in the *i*th column of **c**.

tdc

Input: the last dimension of the array **c** as declared in the function from which nag_glm_tran_model is called.

Constraint: **tdc** $\geq$ **nclin**.

b[ip]

Input: the parameter estimates computed by using the singular value decomposition, $\hat{\beta}_{svd}$.

Output: the parameter estimates of the parameters with the constraints imposed, $\hat{\beta}_c$.

scale

Input: the estimate of the scale parameter.

For results from nag_glm_normal (g02gac) and nag_glm_gamma (g02gdc) then **scale** is the scale parameter, for the model σ^2 and $\hat{\nu}^{-1}$ respectively.

For results from nag_glm_binomial (g02gbc) and nag_glm_poisson (g02gcc) then **scale** should be set to 1.0.

Constraint: **scale** $>$ 0.0.

se[ip]

Output: the standard error of the parameter estimates in **b**.

cov[(ip*(ip+1)/2)]

Output: the upper triangular part of the variance-covariance matrix of the **ip** parameter estimates given in **b**. They are stored packed by column, i.e., the covariance between the parameter estimate given in **b**[*i*] and the parameter estimate given in **b**[*j*], *j* $\geq$ *i*, is stored in **cov**[*j*(*j*+1)/2 + *i*], for *i* = 0, 1, ..., **ip** - 1 and *j* = *i*, *i* + 1, ..., **ip** - 1.

fail

The NAG error parameter, see the Essential Introduction to the NAG C Library.

5. Error Indications and Warnings

NE_INT_ARG_LT

On entry, **ip** must not be less than 1: **ip** = *<value>*.

NE_INT_ARG_LE

On entry, **nclin** must not be less than or equal to 0: **nclin** = *<value>*.

NE_2_INT_ARG_GE

On entry, **nclin** = *<value>* while **ip** = *<value>*. These parameters must satisfy **nclin** $<$ **ip**.

NE_2_INT_ARG_LT

On entry, **tdv** = *<value>* while **ip** = *<value>*. These parameters must satisfy **tdv** $\geq$ **ip**+6.

On entry, **tdc** = *<value>* while **nclin** = *<value>*. These parameters must satisfy **tdc** $\geq$ **nclin**.

NE_REAL_ARG_LE

On entry, **scale** must not be less than or equal to 0.0: **scale** = *<value>*.

NE_MAT_NOT_FULL_RANK

Matrix **c** does not give a model of full rank.

NE_ALLOC_FAIL

Memory allocation failed.

6. Further Comments

This function is intended for use in situations in which dummy (0-1) variables have been used such as in the analysis of designed experiments when the user does not wish to change the parameters of the model to give a full rank model. The function is not intended for situations in which the relationships between the independent variables are only approximate.

6.1. Accuracy

It should be noted that due to rounding errors a parameter that should be zero when the constraints have been imposed may be returned as a value of order **machine precision**.

6.2. References

Golub G H and Van Loan C F (1983) *Matrix Computations* Johns Hopkins University Press, Baltimore.
 McCullagh P and Nelder J A (1983) *Generalized Linear Models* Chapman and Hall.
 Searle S R (1971) *Linear Models* Wiley.

7. See Also

nag_glm_normal (g02gac)
 nag_glm_binomial (g02gbc)
 nag_glm_poisson (g02gcc)
 nag_glm_gamma (g02gdc)
 nag_glm_est_func (g02gnc)

8. Example

A loglinear model is fitted to a 3 by 5 contingency table by nag_glm_poisson (g02gcc). The model consists of terms for rows and columns. The table is:

141	67	114	79	39
131	66	143	72	35
36	14	38	28	16

The constraints that the sum of row effects and the sum of column effects are zero are then read in and the parameter estimates with these constraints imposed are computed by nag_glm_tran_model and printed.

8.1. Program Text

```
/* nag_glm_tran_model(g02gkc) Example Program.
 *
 * Copyright 1996 Numerical Algorithms Group.
 *
 * Mark 4, 1996.
 *
 */
#include <nag.h>
#include <stdio.h>
#include <nag_stdlib.h>
#include <nagg02.h>

#define NMAX 15
#define MMAX 9
#define TDC MMAX
#define TDX MMAX
#define TDV MMAX+6

main()
{
  Integer i, nclin, ip, j, m, n;
  double ex_power;
  Integer sx[MMAX];
  double b[MMAX], c[NMAX][MMAX], cov[MMAX*(MMAX+1)/2], se[MMAX],
    v[NMAX][TDV], x[NMAX][MMAX], y[NMAX];
```

```

double *wtptr;
Integer max_iter;
Integer print_iter;
double eps;
double tol;
double df;
double dev;
Integer rank;
static NagError fail;

Vprintf("g02gkc Example Program Results\n\n");
/* Skip heading in data file */
Vscanf("%*[^\\n]");
Vscanf("%ld %ld %ld", &n, &m, &print_iter);

if (n<=NMAX && m<MMAX)
{
    wtptr = (double *)0;
    for (i=0; i<n; i++)
    {
        for (j=0; j<m; j++)
            Vscanf("%lf", &x[i][j]);
        Vscanf("%lf", &y[i]);
    }
    for (j=0; j<m; j++)
        Vscanf("%ld", &sx[j]);
    Vscanf("%ld", &ip);

    /* Set control parameters */
    max_iter = 10;
    tol = 5e-5;
    eps = 1e-6;
    ex_power = 0.0;
    /* Fit Log-linear model using g02gcc */

    g02gcc(Nag_Log, Nag_MeanInclude, n, (double *)x, (Integer)TDX,
           m, sx, ip, y, wtptr, (double *)0, ex_power, &dev, &df, b, &rank, se, cov,
    (double *)v,
           (Integer)TDV, tol, max_iter, print_iter, "", eps, &fail);

    if (fail.code == NE_NOERROR || fail.code == NE_LSQ_ITER_NOT_CONV ||
        fail.code == NE_RANK_CHANGED || fail.code == NE_ZERO_DOF_ERROR)
    {
        Vprintf("\nDeviance = %12.4e\n", dev);
        Vprintf("Degrees of freedom = %3.1f\n\n", df);
        /* Input constraints */
        nclin = ip - rank;
        for (i=0; i<ip; ++i)
            for (j=0; j<nclin; ++j)
                Vscanf("%lf", &c[i][j]);

        g02gkc(ip, nclin, (double *)v, (Integer)TDV, (double *)c,
               (Integer)TDC, b, 1.0e0, se, cov, &fail);

        if (fail.code == NE_NOERROR)
        {
            Vprintf("      Estimate      Standard error\n\n");
            for (i=0; i<ip; i++)
                Vprintf(" %14.4f%14.4f\n", b[i], se[i]);
            Vprintf("\n");
        }
        else
        {
            Vprintf("%s\n", fail.message);
            exit(EXIT_FAILURE);
        }
    }
    else
    {
        Vprintf("%s\n", fail.message);
    }
}

```

```

        exit(EXIT_FAILURE);
    }
}
else
{
    Vfprintf(stderr, "One or both of m and n are out of range:\n
m = %-3ld while n = %-3ld\n", m, n);
    exit(EXIT_FAILURE);
}
exit(EXIT_SUCCESS);
}

```

8.2. Program Data

```

g02gkc Example Program Data
15 8 0
1.0 0.0 0.0 1.0 0.0 0.0 0.0 0.0 141.
1.0 0.0 0.0 0.0 1.0 0.0 0.0 0.0 67.
1.0 0.0 0.0 0.0 0.0 1.0 0.0 0.0 114.
1.0 0.0 0.0 0.0 0.0 0.0 1.0 0.0 79.
1.0 0.0 0.0 0.0 0.0 0.0 0.0 1.0 39.
0.0 1.0 0.0 1.0 0.0 0.0 0.0 0.0 131.
0.0 1.0 0.0 0.0 1.0 0.0 0.0 0.0 66.
0.0 1.0 0.0 0.0 0.0 1.0 0.0 0.0 143.
0.0 1.0 0.0 0.0 0.0 0.0 1.0 0.0 72.
0.0 1.0 0.0 0.0 0.0 0.0 0.0 1.0 35.
0.0 0.0 1.0 1.0 0.0 0.0 0.0 0.0 36.
0.0 0.0 1.0 0.0 1.0 0.0 0.0 0.0 14.
0.0 0.0 1.0 0.0 0.0 1.0 0.0 0.0 38.
0.0 0.0 1.0 0.0 0.0 0.0 1.0 0.0 28.
0.0 0.0 1.0 0.0 0.0 0.0 0.0 1.0 16.
1 1 1 1 1 1 1 1 9
0.0 0.0
1.0 0.0
1.0 0.0
1.0 0.0
0.0 1.0
0.0 1.0
0.0 1.0
0.0 1.0
0.0 1.0
0.0 1.0

```

8.3. Program Results

```

g02gkc Example Program Results

```

```

Deviance = 9.0379e+00
Degrees of freedom = 8.0

```

Estimate	Standard error
3.9831	0.0396
0.3961	0.0458
0.4118	0.0457
-0.8079	0.0622
0.5112	0.0562
-0.2285	0.0727
0.4680	0.0569
-0.0316	0.0675
-0.7191	0.0887