F07QWF (CSPTRI/ZSPTRI) - NAG Fortran Library Routine Document

Note. Before using this routine, please read the Users' Note for your implementation to check the interpretation of bold italicised terms and other implementation-dependent details.

1 Purpose

F07QWF (CSPTRI/ZSPTRI) computes the inverse of a complex symmetric matrix A, where A has been factorized by F07QRF (CSPTRF/ZSPTRF), using packed storage.

2 Specification

SUBROUTINE F07QWF(UPLO, N, AP, IPIV, WORK, INFO)ENTRYcsptri(UPLO, N, AP, IPIV, WORK, INFO)INTEGERN, IPIV(*), INFOcomplexAP(*), WORK(*)CHARACTER*1UPLO

The ENTRY statement enables the routine to be called by its LAPACK name.

3 Description

To compute the inverse of a complex symmetric matrix A, this routine must be preceded by a call to F07QRF (CSPTRF/ZSPTRF), which computes the Bunch–Kaufman factorization of A using packed storage.

If UPLO = 'U', $A = PUDU^T P^T$ and A^{-1} is computed by solving $U^T P^T X P U = D^{-1}$. If UPLO = 'L', $A = PLDL^T P^T$ and A^{-1} is computed by solving $L^T P^T X P L = D^{-1}$.

4 References

 Du Croz J J and Higham N J (1992) Stability of methods for matrix inversion IMA J. Numer. Anal. 12 1–19

5 Parameters

1: UPLO — CHARACTER*1

On entry: indicates how A has been factorized as follows:

if UPLO = 'U', then $A = PUDU^T P^T$, where U is upper triangular; if UPLO = 'L', then $A = PLDL^T P^T$, where L is lower triangular.

Constraint: UPLO = 'U' or 'L'.

```
2: N — INTEGER
```

On entry: n, the order of the matrix A.

Constraint: $N \ge 0$.

3: AP(*) - complex array

Note: the dimension of the array AP must be at least $\max(1, N*(N+1)/2)$.

On entry: details of the factorization of A stored in packed form, as returned by F07QRF (CSPTRF/ZSPTRF).

On exit: the factorization is overwritten by the n by n symmetric matrix A^{-1} stored in packed form. More precisely, the (i, j)th element of A^{-1} is stored in AP(i + j(j - 1)/2) for $i \le j$ if UPLO = 'U', and in AP(i + (2n - j)(j - 1)/2) for $i \ge j$ if UPLO = 'L'.

Input

Input

Input/Output

Input

Output

4: IPIV(*) — INTEGER array

Note: the dimension of the array IPIV must be at least $\max(1,N)$.

On entry: details of the interchanges and the block structure of D, as returned by F07QRF (CSPTRF/ZSPTRF).

5: WORK(*) — complex array Workspace

Note: the dimension of the array WORK must be at least $\max(1,N)$.

6: INFO — INTEGER

On exit: INFO = 0 unless the routine detects an error (see Section 6).

6 Error Indicators and Warnings

$\mathrm{INFO} < 0$

If INFO = -i, the *i*th parameter had an illegal value. An explanatory message is output, and execution of the program is terminated.

INFO > 0

If INFO = i, d_{ii} is exactly zero; D is singular and the inverse of A cannot be computed.

7 Accuracy

The computed inverse \boldsymbol{X} satisfies a bound of the form

 $|DU^T P^T X P U - I| \le c(n)\epsilon(|D||U^T|P^T|X|P|U| + |D||D^{-1}|) \quad \text{if UPLO} = \text{'U', or} \\ |DL^T P^T X P L - I| \le c(n)\epsilon(|D||L^T|P^T|X|P|L| + |D||D^{-1}|) \quad \text{if UPLO} = \text{'L',}$

where c(n) is a modest linear function of n, and ϵ is the *machine precision*.

8 Further Comments

The total number of real floating-point operations is approximately $\frac{8}{3}n^3$.

The real analogue of this routine is F07PJF (SSPTRI/DSPTRI).

9 Example

To compute the inverse of the matrix A, where

$A = \left(\right)$	-0.39 - 0.71i	5.14 - 0.64i	-7.86 - 2.96i	3.80 + 0.92i
	5.14 - 0.64i	8.86 + 1.81i	-3.52 + 0.58i	5.32 - 1.59i
	-7.86 - 2.96i	-3.52 + 0.58i	-2.83 - 0.03i	-1.54 - 2.86i
	3.80 + 0.92i	5.32 - 1.59i	-1.54 - 2.86i	-0.56 + 0.12i

Here A is symmetric, stored in packed form, and must first be factorized by F07QRF (CSPTRF/ZSPTRF).

9.1 Program Text

Note. The listing of the example program presented below uses bold italicised terms to denote precision-dependent details. Please read the Users' Note for your implementation to check the interpretation of these terms. As explained in the Essential Introduction to this manual, the results produced may not be identical for all implementations.

```
F07QWF Example Program Text
*
     Mark 15 Release. NAG Copyright 1991.
*
      .. Parameters ..
*
      INTEGER
                       NIN, NOUT
     PARAMETER
                       (NIN=5,NOUT=6)
     INTEGER
                      NMAX
     PARAMETER
                      (NMAX=8)
      .. Local Scalars ..
*
     INTEGER I, IFAIL, INFO, J, N
                     UPLO
      CHARACTER
      .. Local Arrays ..
                      AP(NMAX*(NMAX+1)/2), WORK(NMAX)
      complex
      INTEGER
                       IPIV(NMAX)
     CHARACTER
                       CLABS(1), RLABS(1)
      .. External Subroutines ..
     EXTERNAL
                       csptrf, csptri, X04DDF
      .. Executable Statements ..
     WRITE (NOUT,*) 'FO7QWF Example Program Results'
     Skip heading in data file
     READ (NIN,*)
     READ (NIN,*) N
      IF (N.LE.NMAX) THEN
         Read A from data file
         READ (NIN,*) UPLO
         IF (UPLO.EQ.'U') THEN
            READ (NIN,*) ((AP(I+J*(J-1)/2),J=I,N),I=1,N)
         ELSE IF (UPLO.EQ.'L') THEN
            READ (NIN,*) ((AP(I+(2*N-J)*(J-1)/2),J=1,I),I=1,N)
         END IF
         Factorize A
*
         CALL csptrf(UPLO, N, AP, IPIV, INFO)
         WRITE (NOUT,*)
         IF (INFO.EQ.O) THEN
            Compute inverse of A
            CALL csptri(UPLO, N, AP, IPIV, WORK, INFO)
*
            Print inverse
*
            IFAIL = 0
            CALL X04DDF(UPLO, 'Nonunit', N, AP, 'Bracketed', 'F7.4',
     +
                        'Inverse', 'Integer', RLABS, 'Integer', CLABS, 80,0,
                        IFAIL)
     +
         ELSE
            WRITE (NOUT,*) 'The factor D is singular'
         END IF
     END IF
      STOP
```

END

*

9.2 Program Data

 F07QWF Example Program Data
 :Value of N

 4
 :Value of UPLO

 'L'
 :Value of UPLO

 (-0.39,-0.71)
 :Value of UPLO

 (5.14,-0.64) (8.86, 1.81)
 :-2.83,-0.03)

 (-7.86,-2.96) (-3.52, 0.58) (-2.83,-0.03)
 :End of matrix A

9.3 Program Results

F07QWF Example Program Results

Inverse