F08GEF (SSPTRD/DSPTRD) – NAG Fortran Library Routine Document

Note. Before using this routine, please read the Users' Note for your implementation to check the interpretation of bold italicised terms and other implementation-dependent details.

1 Purpose

F08GEF (SSPTRD/DSPTRD) reduces a real symmetric matrix to tridiagonal form, using packed storage.

2 Specification

SUBROUTINE F08GEF(UPLO, N, AP, D, E, TAU, INFO)ENTRYssptrd(UPLO, N, AP, D, E, TAU, INFO)INTEGERN, INFOrealAP(*), D(*), E(*), TAU(*)CHARACTER*1UPLO

The ENTRY statement enables the routine to be called by its LAPACK name.

3 Description

This routine reduces a real symmetric matrix A, held in packed storage, to symmetric tridiagonal form T by an orthogonal similarity transformation: $A = QTQ^{T}$.

The matrix Q is not formed explicitly but is represented as a product of n-1 elementary reflectors (see the Chapter Introduction for details). Routines are provided to work with Q in this representation (see Section 8).

4 References

 Golub G H and van Loan C F (1996) Matrix Computations Johns Hopkins University Press (3rd Edition), Baltimore

5 Parameters

1: UPLO — CHARACTER*1

On entry: indicates whether the upper or lower triangular part of A is stored as follows:

if UPLO = 'U', then the upper triangular part of A is stored;

if UPLO = L', then the lower triangular part of A is stored.

Constraint: UPLO = 'U' or 'L'.

```
2: N — INTEGER
```

On entry: n, the order of the matrix A.

Constraint: $N \ge 0$.

3: AP(*) - real array

Note: the dimension of the array AP must be at least $\max(1, N*(N+1)/2)$.

On entry: the n by n symmetric matrix A, packed by columns. More precisely, if UPLO = 'U', the upper triangle of A must be stored with element a_{ij} in AP(i + j(j - 1)/2) for $i \leq j$; if UPLO = 'L', the lower triangle of A must be stored with element a_{ij} in AP(i + (2n - j)(j - 1)/2) for $i \geq j$.

On exit: A is overwritten by the tridiagonal matrix T and details of the orthogonal matrix Q.

Input

Input

Input/Output

4:	$\mathrm{D}(*)-real$ array	Output
	Note: the dimension of the array D must be at least $\max(1,N)$.	
	On exit: the diagonal elements of the tridiagonal matrix T .	
5:	$\mathrm{E}(*) - \boldsymbol{real}$ array	Output
	Note: the dimension of the array E must be at least $\max(1, N-1)$.	
	On exit: the off-diagonal elements of the tridiagonal matrix T .	
6:	TAU(*) - real array	Output
	Note: the dimension of the array TAU must be at least $\max(1, N-1)$.	
	On exit: further details of the orthogonal matrix Q .	
7:	INFO — INTEGER	Output
	On exit: $INFO = 0$ unless the routine detects an error (see Section 6).	

6 Error Indicators and Warnings

INFO < 0

If INFO = -i, the *i*th parameter had an illegal value. An explanatory message is output, and execution of the program is terminated.

7 Accuracy

The computed tridiagonal matrix T is exactly similar to a nearby matrix A + E, where

 $\parallel E \parallel_2 \le c(n)\epsilon \parallel A \parallel_2,$

c(n) is a modestly increasing function of n, and ϵ is the *machine precision*.

The elements of T themselves may be sensitive to small perturbations in A or to rounding errors in the computation, but this does not affect the stability of the eigenvalues and eigenvectors.

8 Further Comments

The total number of floating-point operations is approximately $\frac{4}{3}n^3$.

To form the orthogonal matrix Q this routine may be followed by a call to F08GFF (SOPGTR/DOPGTR):

CALL SOPGTR (UPLO,N,AP,TAU,Q,LDQ,WORK,INFO)

To apply Q to an n by p real matrix C this routine may be followed by a call to F08GGF (SOPMTR/DOPMTR). For example,

CALL SOPMTR ('Left', UPLO, 'No Transpose', N, P, AP, TAU, C, LDC, WORK, + INFO)

forms the matrix product QC.

The complex analogue of this routine is F08GSF (CHPTRD/ZHPTRD).

9 Example

To reduce the matrix A to tridiagonal form, where

$$A = \begin{pmatrix} 2.07 & 3.87 & 4.20 & -1.15 \\ 3.87 & -0.21 & 1.87 & 0.63 \\ 4.20 & 1.87 & 1.15 & 2.06 \\ -1.15 & 0.63 & 2.06 & -1.81 \end{pmatrix}$$

using packed storage.

9.1 Program Text

Note. The listing of the example program presented below uses bold italicised terms to denote precision-dependent details. Please read the Users' Note for your implementation to check the interpretation of these terms. As explained in the Essential Introduction to this manual, the results produced may not be identical for all implementations.

```
FO8GEF Example Program Text
*
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*
      .. Parameters ..
     INTEGER
                      NIN, NOUT
                      (NIN=5,NOUT=6)
     PARAMETER
     INTEGER
                     NMAX
     PARAMETER
                     (NMAX=8)
      .. Local Scalars ..
     INTEGER
                      I, INFO, J, N
     CHARACTER
                     UPLO
      .. Local Arrays ..
     real
                      AP(NMAX*(NMAX+1)/2), D(NMAX), E(NMAX-1),
                      TAU(NMAX-1)
     +
      .. External Subroutines ..
     EXTERNAL
                      ssptrd
      .. Executable Statements ..
     WRITE (NOUT,*) 'FO8GEF Example Program Results'
     Skip heading in data file
     READ (NIN,*)
     READ (NIN,*) N
     IF (N.LE.NMAX) THEN
        Read A from data file
        READ (NIN,*) UPLO
        IF (UPLO.EQ.'U') THEN
           READ (NIN,*) ((AP(I+J*(J-1)/2),J=I,N),I=1,N)
        ELSE IF (UPLO.EQ.'L') THEN
            READ (NIN,*) ((AP(I+(2*N-J)*(J-1)/2),J=1,I),I=1,N)
        END IF
        Reduce A to tridiagonal form
*
        CALL ssptrd(UPLO, N, AP, D, E, TAU, INFO)
*
*
        Print tridiagonal form
*
        WRITE (NOUT,*)
        WRITE (NOUT, *) 'Diagonal'
        WRITE (NOUT,99999) (D(I),I=1,N)
        WRITE (NOUT, *) 'Off-diagonal'
        WRITE (NOUT, 99999) (E(I), I=1, N-1)
     END IF
```

```
STOP
*
99999 FORMAT (1X,8F9.4)
END
```

9.2 Program Data

 F08GEF Example Program Data

 4
 :Value of N

 'L'
 :Value of UPLO

 2.07
 .87
 -0.21

 4.20
 1.87
 1.15

 -1.15
 0.63
 2.06
 -1.81
 :End of matrix A

9.3 Program Results

FO8GEF Example Program Results

Diagonal 2.0700 1.4741 -0.6492 -1.6949 Off-diagonal -5.8258 2.6240 0.9163