

## Meaning of prefixes

S - REAL  
D - DOUBLE PRECISION

C - COMPLEX  
Z - COMPLEX16  
(this may not be supported by all machines)

For the Level 2 BLAS a set of extended precision routines with the prefixes **ED**, **EDC**, **EZ** may also be available.

## Level 1 BLAS

In addition to the listed routines there are two further extended precision dot product routines **DQDOTI** and **DQDMA**.

## Level 2 and Level 3 BLAS

Matrix types:

GE- General	CB- General Band
SY - Symmetric	SB- Sym Band
HE- Hermitian	HB- Herm Band
TR- Triangular	TB- Triang Band

SP- Sum Packed
HP- Herm Packed
TP- Triang Packed

## Level 2 and Level 3 BLAS Options

Many options arguments are declared as **CHAR\*1** and may be passed as character strings.

<b>TRANS</b>	= 'No transpose', 'Transpose', 'Conjugate transpose' ( $X, X^T, X^H$ )
<b>UHO</b>	= 'Upper triangular', 'Lower triangular'
<b>DAG</b>	= 'Non-unit triangular', 'Unit triangular'
<b>SIDE</b>	= 'Left', 'Right' (A or op(A) on the left, or A or op(A) on the right)

For real matrices, **TRANS** = 'T' and **TRANS** = 'C' have the same meaning.

For Hermitian matrices, **TRANS** = 'T' is not allowed.

For complex symmetric matrices, **TRANS** = 'H' is not allowed.

## References

C Lawson, R Hanson, D Kincaid, and F Krogh, "Basic Linear Algebra Subprograms for Fortran Usage," *ACM Trans. on Math. Soft.* 5 (1979) 308-325

J.J. Dongarra, J. Dongarra, S. Hamerling, and R. Hanson, "An Extended Set of Fortran Basic Linear Algebra Subprograms," *ACM Trans. on Math. Soft.* 14,1 (1988) 1-32

J.J. Dongarra, I. Duff, J. Dongarra, and S. Hamerling, "A Set of Level 3 Basic Linear Algebra Subprograms," *ACM Trans. on Math. Soft.* 16,1 (1990) 1-28

## Obtaining the Software via [netlib@ornl.gov](mailto:netlib@ornl.gov)

To receive a copy of the single-precision software, type in a mail message:

```
send sblas from blas
send sblas2 from blas
send sblas3 from blas
```

To receive a copy of the double-precision software, type in a mail message:

```
send dblas from blas
send dblas2 from blas
send dblas3 from blas
```

To receive a copy of the complex single-precision software, type in a mail message:

```
send cblas from blas
send cblas2 from blas
send cblas3 from blas
```

To receive a copy of the complex double-precision software, type in a mail message:

```
send zblas from blas
send zblas2 from blas
send zblas3 from blas
```

Send comments and questions to [lapack@cs.utk.edu](mailto:lapack@cs.utk.edu).

# Basic

# Linear

# Algebra

# Subprograms

# A Quick Reference Guide

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Level 1 BLAS

```

        dim scalar vector    vector    scalars      5-element array
SUBROUTINE xROTG (                                A, B, C, S )
SUBROUTINE xROTMG(                               D1, D2, A, B,      PARAM )
SUBROUTINE xROT (  N,           X, INCX, Y, INCY,      C, S )
SUBROUTINE xROTM ( N,           X, INCX, Y, INCY,      PARAM )
SUBROUTINE xSWAP ( N,           X, INCX, Y, INCY )
SUBROUTINE xSCAL ( N,   ALPHA, X, INCX )
SUBROUTINE xCOPY ( N,           X, INCX, Y, INCY )
SUBROUTINE xAXPY ( N,   ALPHA, X, INCX, Y, INCY )
FUNCTION  xDOT ( N,           X, INCX, Y, INCY )
FUNCTION  xDOTU ( N,           X, INCX, Y, INCY )
FUNCTION  xDOTC ( N,           X, INCX, Y, INCY )
FUNCTION  xxDOT ( N,   ALPHA, X, INCX, Y, INCY )
FUNCTION  xWRM2 ( N,           X, INCX )
FUNCTION  xASUM ( N,           X, INCX )
FUNCTION  IxAMAX( N,           X, INCX )

```

Level 2 BLAS

options	dim	b-width	scalar	matrix	vector	scalar	vector
xGEMV ( TRANS,	M, N,		ALPHA, A, LDA, X, INCX, BETA, Y, INCY )				
xGBMV ( TRANS,	M, N, KL, KU,		ALPHA, A, LDA, X, INCX, BETA, Y, INCY )				
xHEMV ( UPLO,	N,		ALPHA, A, LDA, X, INCX, BETA, Y, INCY )				
xHBMV ( UPLO,	N, K,		ALPHA, A, LDA, X, INCX, BETA, Y, INCY )				
xHPMV ( UPLO,	N,		ALPHA, AP, X, INCX, BETA, Y, INCY )				
xSYMV ( UPLO,	N,		ALPHA, A, LDA, X, INCX, BETA, Y, INCY )				
xSBMV ( UPLO,	N, K,		ALPHA, A, LDA, X, INCX, BETA, Y, INCY )				
xSPMV ( UPLO,	N,		ALPHA, AP, X, INCX, BETA, Y, INCY )				
xTRMV ( UPLO, TRANS, DIAG,	N,		A, LDA, X, INCX )				
xTBMV ( UPLO, TRANS, DIAG,	N, K,		A, LDA, X, INCX )				
xTPMV ( UPLO, TRANS, DIAG,	N,		AP, X, INCX )				
xTRSV ( UPLO, TRANS, DIAG,	N,		A, LDA, X, INCX )				
xTBSV ( UPLO, TRANS, DIAG,	N, K,		A, LDA, X, INCX )				
xTPSV ( UPLO, TRANS, DIAG,	N,		AP, X, INCX )				
options	dim	scalar	vector	vector	matrix		
xGER (	M, N, ALPHA, X, INCX, Y, INCY, A, LDA )						
xGERU (	M, N, ALPHA, X, INCX, Y, INCY, A, LDA )						
xGERC (	M, N, ALPHA, X, INCX, Y, INCY, A, LDA )						
xHER ( UPLO,	N, ALPHA, X, INCX,				A, LDA )		
xHPR ( UPLO,	N, ALPHA, X, INCX,				AP )		
xHER2 ( UPLO,	N, ALPHA, X, INCX, Y, INCY, A, LDA )						
xHPR2 ( UPLO,	N, ALPHA, X, INCX, Y, INCY, AP )						
xSYR ( UPLO,	N, ALPHA, X, INCX,				A, LDA )		
xSPR ( UPLO,	N, ALPHA, X, INCX,				AP )		
xSYR2 ( UPLO,	N, ALPHA, X, INCX, Y, INCY, A, LDA )						
xSPR2 ( UPLO,	N, ALPHA, X, INCX, Y, INCY, AP )						

Level 3 BLAS

options	dim	scalar	matrix	matrix	scalar	matrix
xGEMM ( TRANS <sub>A</sub> , TRANS <sub>B</sub> ,	M, N, K,	ALPHA, A,	LDA, B,	LDB, BETA,	C,	LDC
xSYMM ( SIDE, UPLO,	M, N,	ALPHA, A,	LDA, B,	LDB, BETA,	C,	LDC
xHEMM ( SIDE, UPLO,	M, N,	ALPHA, A,	LDA, B,	LDB, BETA,	C,	LDC
xSYRK ( UPLO, TRANS,	N, K,	ALPHA, A,	LDA,		BETA,	C, LDC
xHERK ( UPLO, TRANS,	N, K,	ALPHA, A,	LDA,		BETA,	C, LDC
xSYR2K( UPLO, TRANS,	N, K,	ALPHA, A,	LDA, B,	LDB, BETA,	C,	LDC
xHER2K( UPLO, TRANS,	N, K,	ALPHA, A,	LDA, B,	LDB, BETA,	C,	LDC
xTRMM ( SIDE, UPLO, TRANS <sub>A</sub> ,	DIAG, M,	N,	ALPHA, A,	LDA, B,	LDB )	
xTRSM ( SIDE, UPLO, TRANS <sub>A</sub> ,	DIAG, M,	N,	ALPHA, A,	LDA, B,	LDB )	

```

Generate plane rotation
Generate modified plane rotation
Apply plane rotation
Apply modified plane rotation
 $x \leftarrow y$ 
 $x \leftarrow \alpha x$ 
 $y \leftarrow x$ 
 $y \leftarrow \alpha x + y$ 
 $dot \leftarrow x^T y$ 
 $dot \leftarrow x^T y$ 
 $dot \leftarrow x^H y$ 
 $dot \leftarrow \alpha x^T y$ 
 $nrm2 \leftarrow \|x_2\|$ 
 $asum \leftarrow \|re(x)\| \|im(x)\|$ 
 $a\ ma\ x \leftarrow \# k \ni |re(x)| + i|im(x)|$ 
 $=ma\ x ((r e_k)x + i m_k x)$ 

```

$y \leftarrow \alpha Ax + \beta y$ ,	$y \leftarrow T_{\alpha A} + \beta y$ ,	$y \leftarrow \alpha^H Ax + \beta y$ ,	$A = m \times n$	S D G Z
$y \leftarrow \alpha Ax + \beta y$ ,	$y \leftarrow T_{\alpha A} + \beta y$ ,	$y \leftarrow \alpha^H Ax + \beta y$ ,	$A = m \times n$	S D G Z
$y \leftarrow \alpha Ax + \beta y$				G Z
$y \leftarrow \alpha Ax + \beta y$				G Z
$y \leftarrow \alpha Ax + \beta y$				C Z
$y \leftarrow \alpha Ax + \beta y$				S D
$y \leftarrow \alpha Ax + \beta y$				S D
$y \leftarrow \alpha Ax + \beta y$				S D
$x \leftarrow Ax$ ,	$x \leftarrow {}^T A$ ,	$x \leftarrow {}^H Ax$		S D C Z
$x \leftarrow Ax$ ,	$x \leftarrow {}^T A$ ,	$x \leftarrow {}^H Ax$		S D C Z
$x \leftarrow Ax$ ,	$x \leftarrow {}^T A$ ,	$x \leftarrow {}^H Ax$		S D C Z
$x \leftarrow A^{-1}x$ ,	$x \leftarrow {}^T A x$ ,	$x \leftarrow {}^H A x$		S D G Z
$x \leftarrow A^{-1}x$ ,	$x \leftarrow {}^T A x$ ,	$x \leftarrow {}^H A x$		S D G Z
$x \leftarrow A^{-1}x$ ,	$x \leftarrow {}^T A x$ ,	$x \leftarrow {}^H A x$		S D G Z
$A \leftarrow \alpha x {}^T y + A$ ,	$A = m \times n$			S D
$A \leftarrow \alpha x {}^T y + A$ ,	$A = m \times n$			G Z
$A \leftarrow \alpha x {}^T y + A$ ,	$A = m \times n$			C Z
$A \leftarrow \alpha x {}^T y + A$				G Z
$A \leftarrow \alpha x {}^T y + A$				C Z
$A \leftarrow \alpha x {}^T y + y (\alpha x {}^T y + A)$				G Z
$A \leftarrow \alpha x {}^T y + y (\alpha x {}^T y + A)$				C Z
$A \leftarrow \alpha x {}^T z + A$				S D
$A \leftarrow \alpha x {}^T z + A$				S D
$A \leftarrow \alpha x {}^T y + \alpha y {}^{x^T} + A$				S D
$A \leftarrow \alpha x {}^T y + \alpha y {}^{x^T} + A$				S D

$C \leftarrow \alpha o p(A)o p(B) + \beta C, o p(X) = X^T, X \bar{X}^H, C - m \times n$	S D G Z
$C \leftarrow \alpha AB + \beta C, C \leftarrow \alpha BA + \beta C, C - m \times n, A \xrightarrow{T} A$	S D G Z
$C \leftarrow \alpha AB + \beta C, C \leftarrow \alpha BA + \beta C, C - m \times n, A \xrightarrow{H} A$	G Z
$C \leftarrow \alpha A \bar{A}^T + \beta C, C \leftarrow \alpha \bar{A}^T A + \beta C, C - n \times n$	S D G Z
$C \leftarrow \alpha A A^H + \beta C, C \leftarrow \alpha A^H A + \beta C, C - n \times n$	G Z
$C \leftarrow \alpha A B^T + \bar{\alpha} B A^T + \beta C, C \leftarrow \alpha \bar{A}^T B + \bar{\alpha} B^T A + \beta C, C - n \times n$	S D G Z
$C \leftarrow \alpha A B^H + \bar{\alpha} B A^H + \beta C, C \leftarrow \alpha A^H B + \bar{\alpha} B^H A + \beta C, C - n \times n$	G Z
$B \leftarrow \alpha o p(A)B, B \leftarrow \alpha B o p(A), o p(A) \xrightarrow{T} A \bar{A}^T A B - m \times n$	S D G Z
$B \leftarrow \alpha o p(A^T)B, B \leftarrow \alpha B o p(\bar{A}), o p(A) = A^T A \bar{A}^T, B - m \times n$	S D G Z